

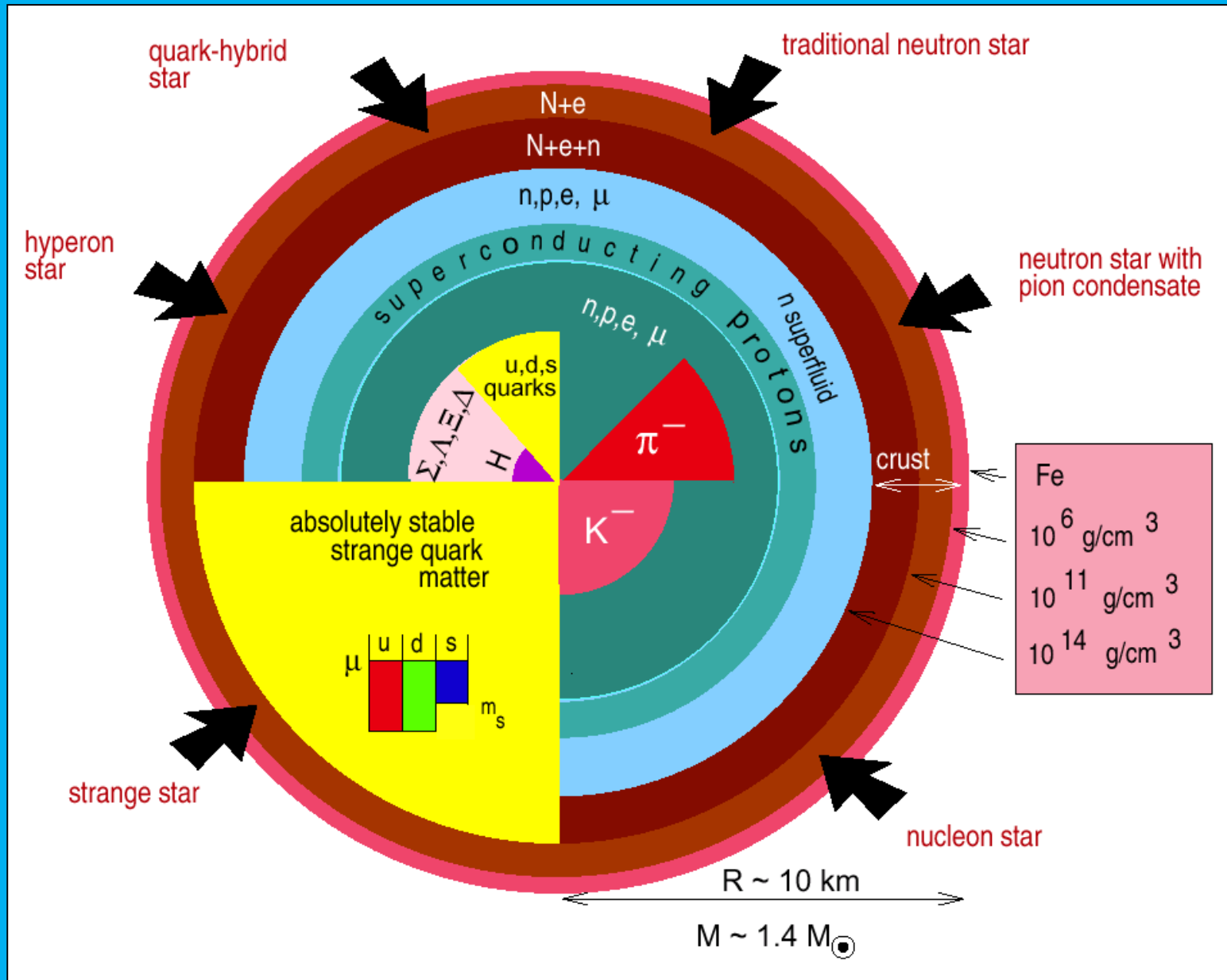
On the possible consequences of multiple phase transitions inside hybrid stars

A. Yudin, T. Razinkova, D. Nadyozhin

The International Conference
SN 1987A, Quark Phase Transition in Compact Objects
and Multimessenger Astronomy

2-8 July 2017

Composition of Neutron Star



Ordinary Phase Transition

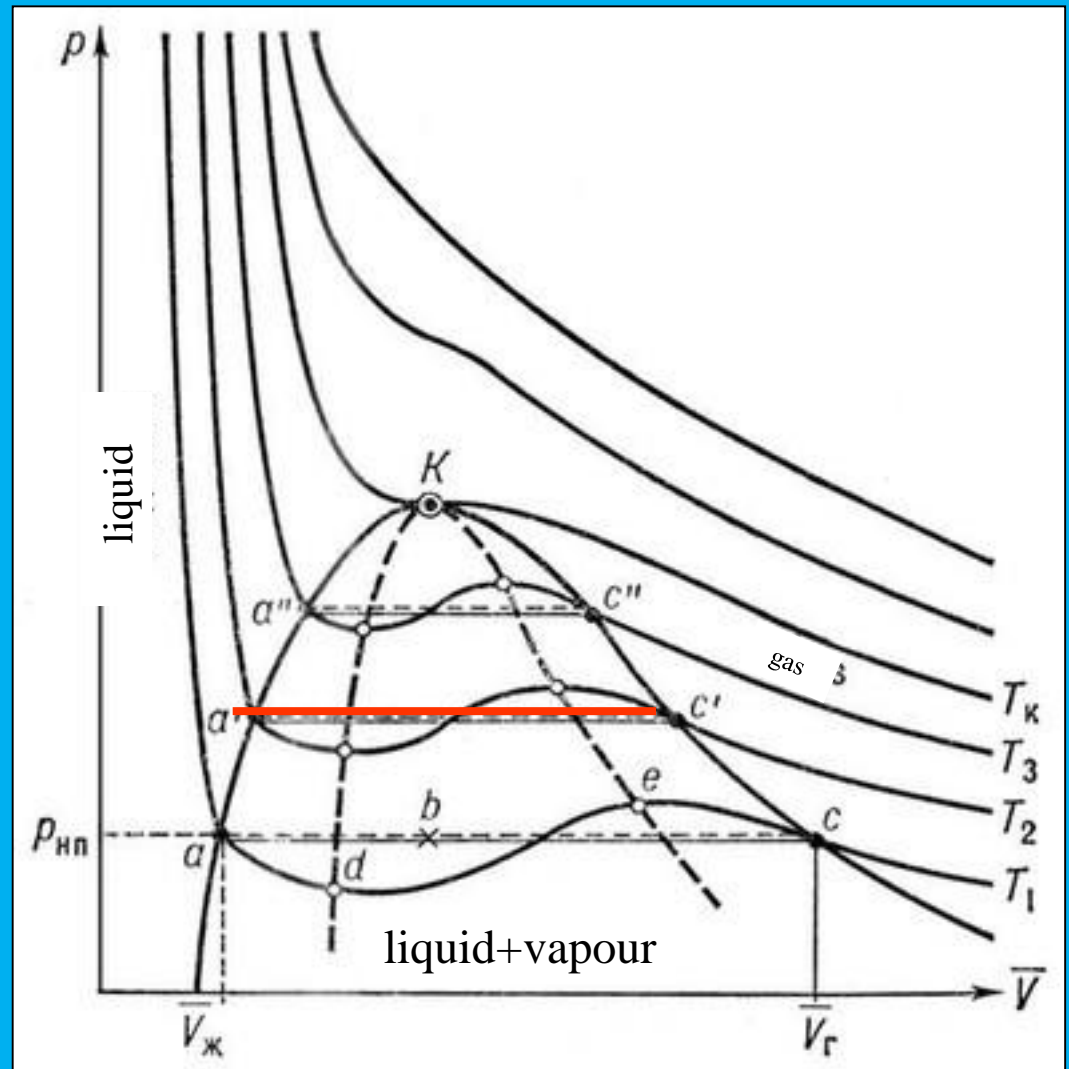
One-component matter
Maxwell-type PT

Phase coexistence conditions:

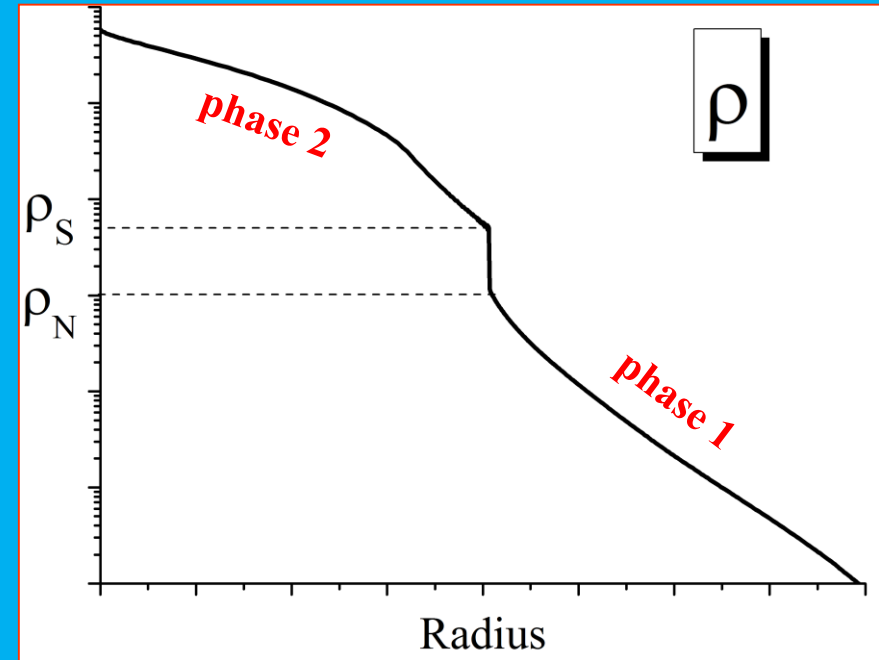
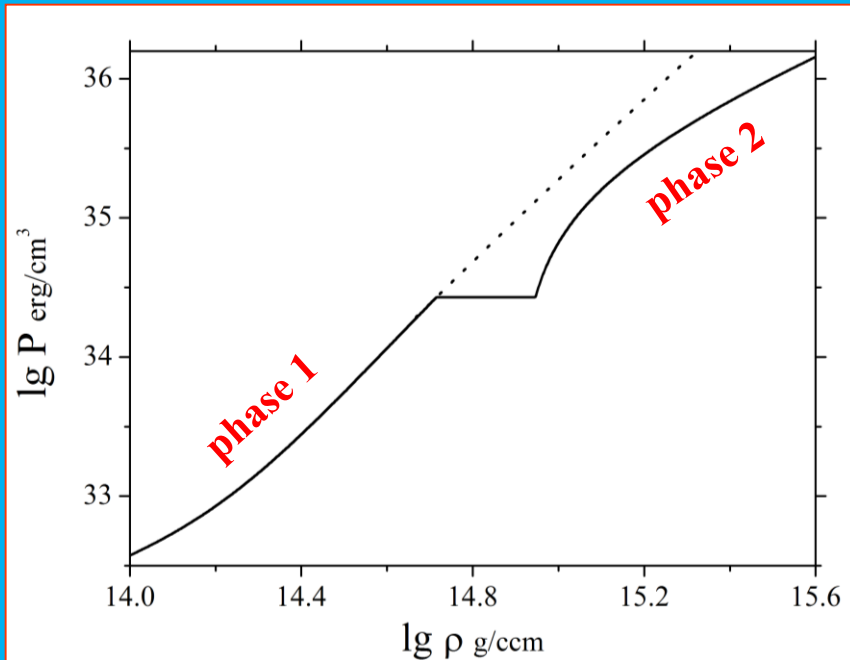
$$\begin{cases} P_I(\rho_I, T) = P_{II}(\rho_{II}, T) \\ \mu_I(\rho_I, T) = \mu_{II}(\rho_{II}, T) \end{cases}$$

$$\rho = \chi\rho_I + (1 - \chi)\rho_{II}$$

$$\chi = \frac{V_I}{V}, \quad V = V_I + V_{II}$$



Maxwellian-type phase transition causes a density jump inside the star



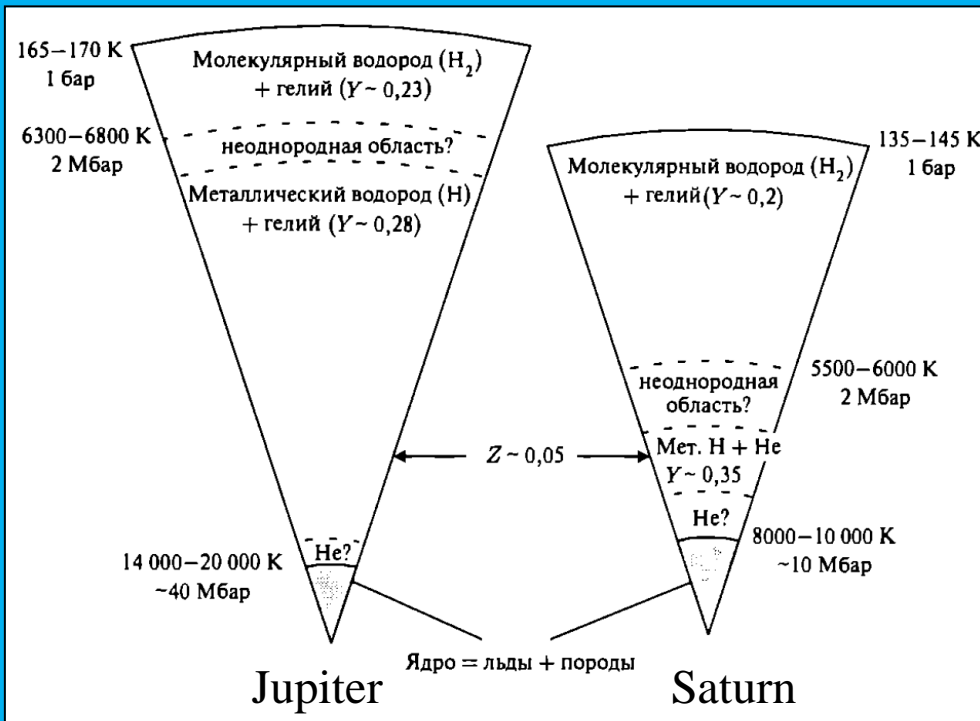
$$\lambda_c = \frac{\rho_S}{\rho_N} = \frac{3}{2}$$

$$\lambda^{rel} = \frac{\epsilon_2}{\epsilon_1}$$

$$\lambda_c^{rel} = \frac{3}{2} \left(1 + \frac{P_*}{\epsilon_1} \right)$$

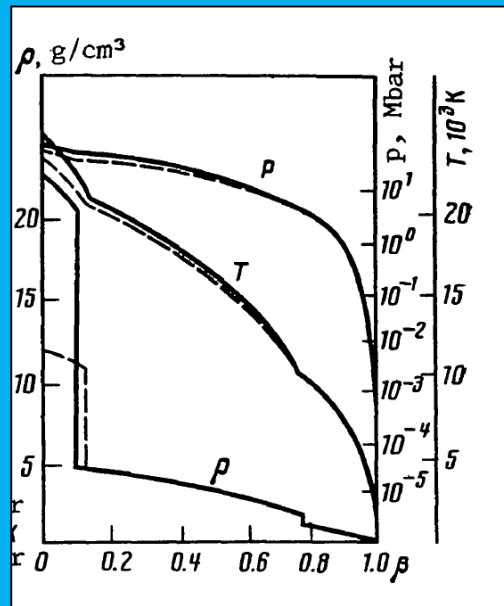
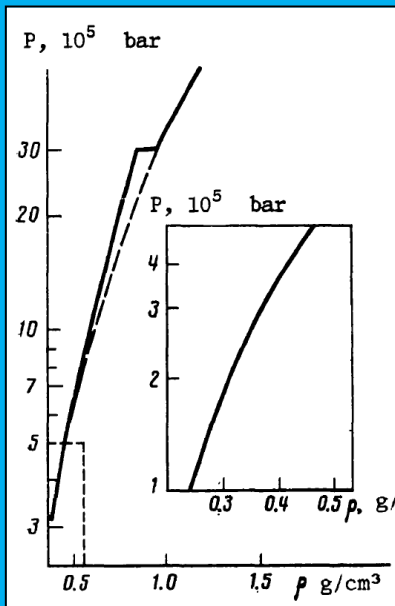
Z.F. Seidov (1971)

W.H. Ramsey, MNRAS 110 (1950) 325
M.J. Lighthill, MNRAS 110 (1950) 339



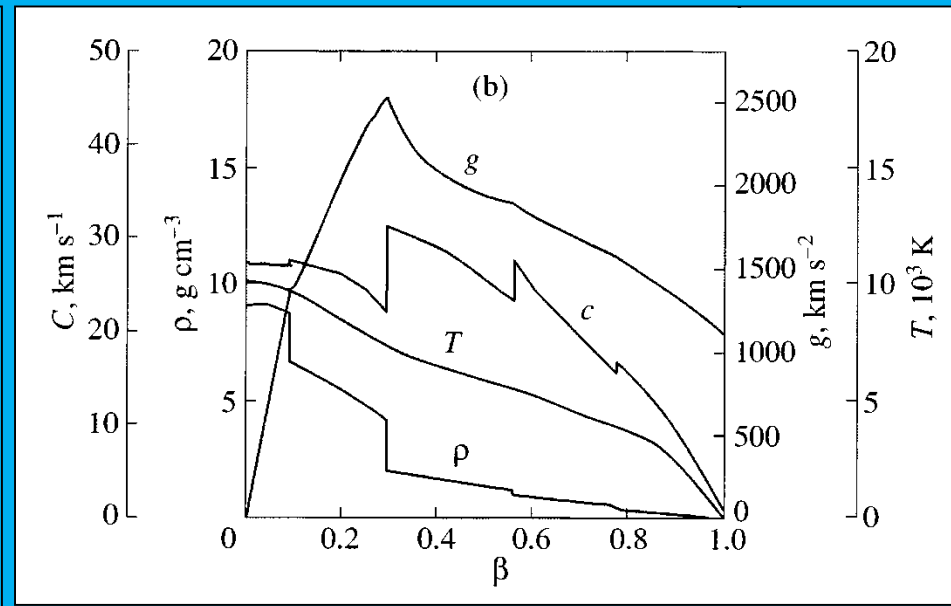
Giant Planets and (maybe?) Brown Dwarfs

From "Systems of Jupiter and Saturn" by
Kuskov, Dorofeeva, Kronrod and Makalkin
URSS 2009 (on russian)



T. V. Gudkova, V. N. Zharkov, and V. V. Leont'ev

Soviet Astronomy Letters, Vol.14, NO. 2/MAR, P. 157, 1988

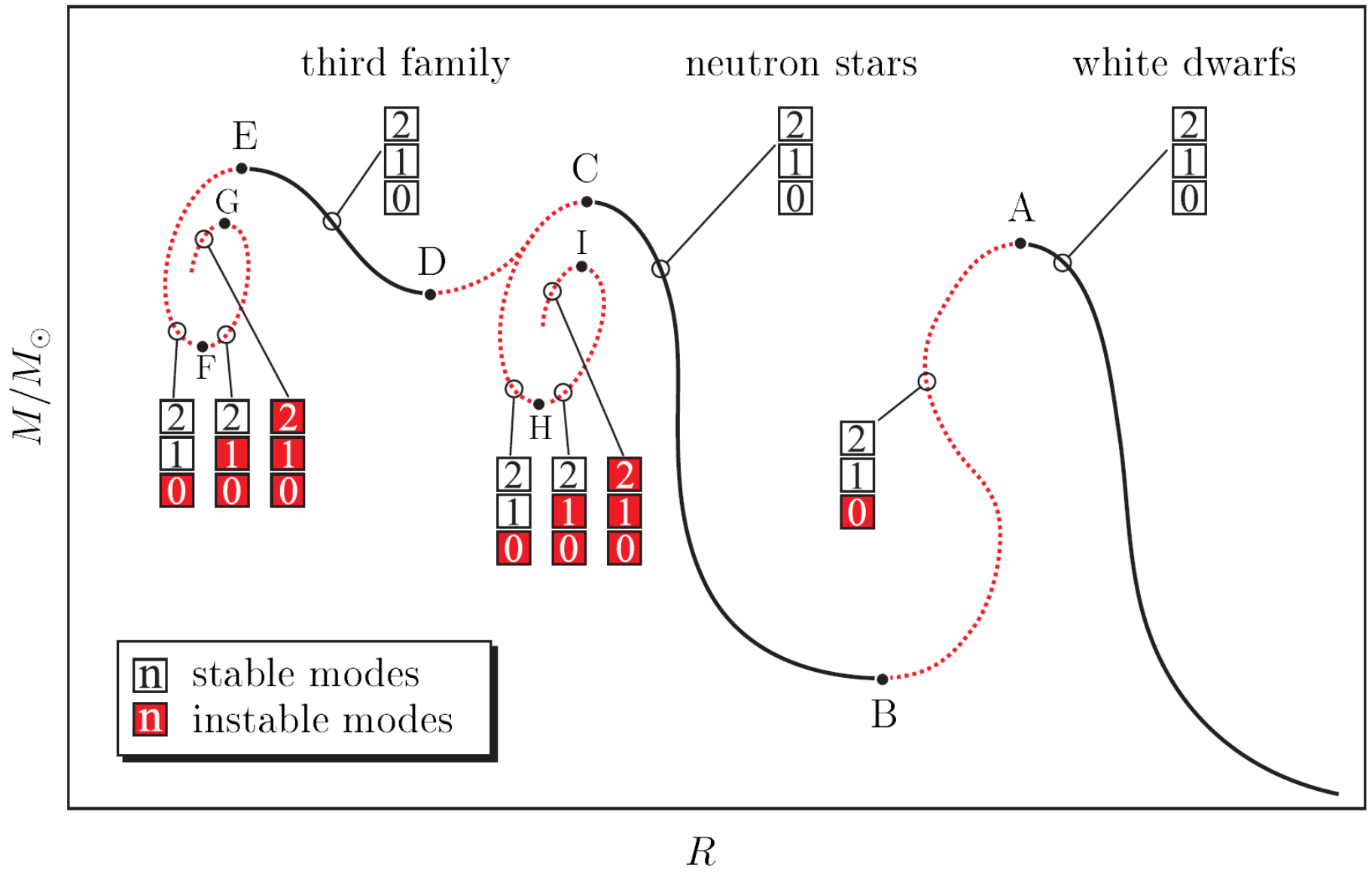


T. V. Gudkova* and V. N. Zharkov

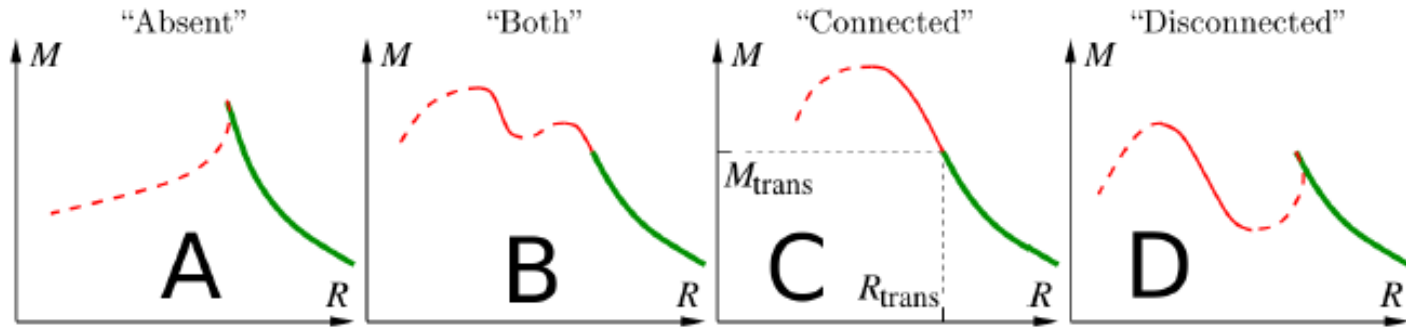
Astronomy Letters, Vol. 29, No. 10, 2003, pp. 674-694.

Quark phases in neutron stars and a
 “third family” of compact stars
 as a signature for phase transitions*

K. Schertler^a, C. Greiner^a, J. Schaffner-Bielich^b, and M.H. Thoma^{c,†}



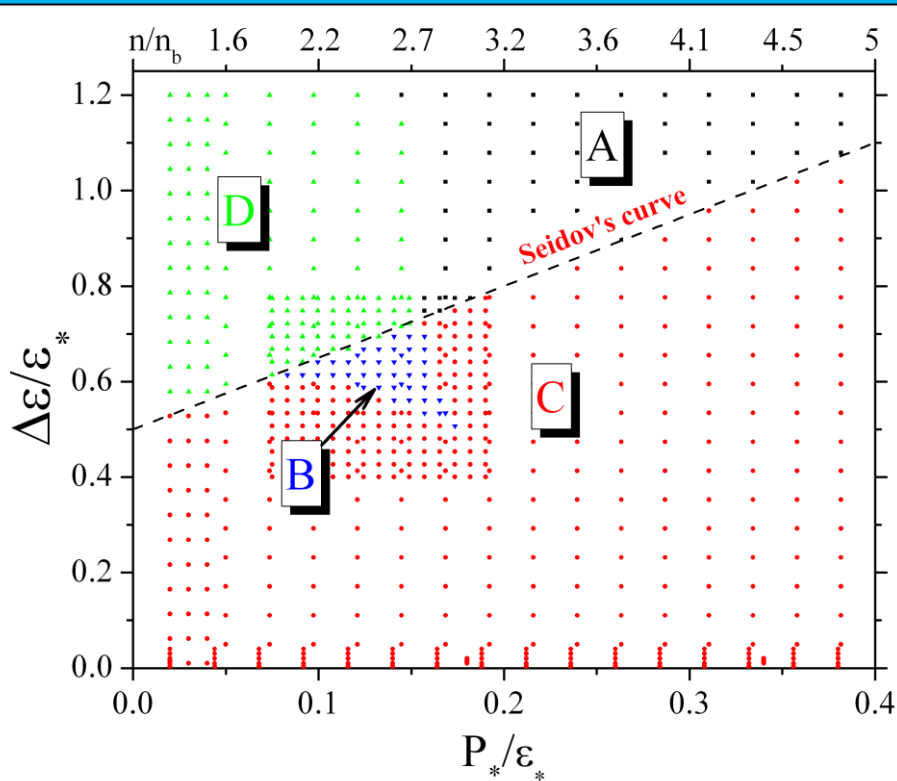
Mass-Radius relations for hybrid stars



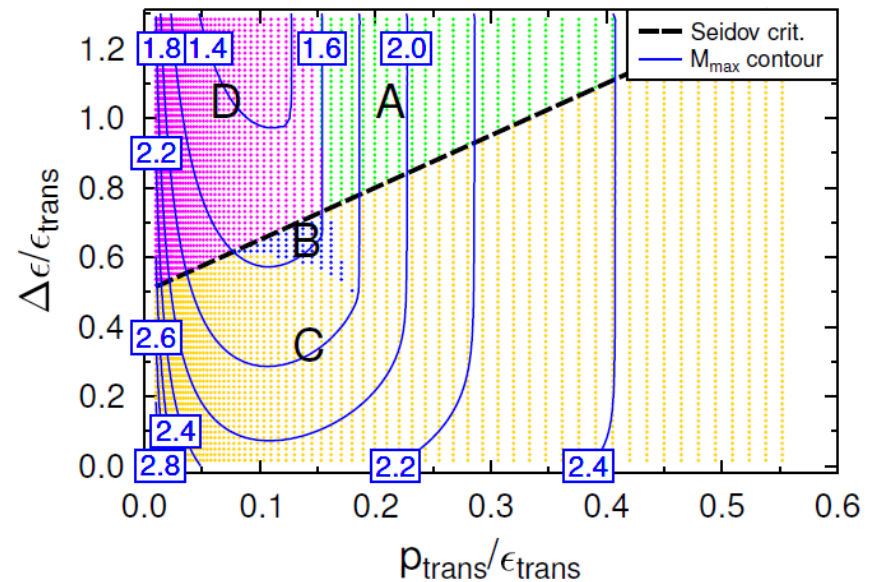
M. G. Alford, S. Han, and M. Prakash, Phys. Rev. D **88**, 083013 (2013).

$$\lambda^{rel} = \frac{\epsilon_2}{\epsilon_1}$$

$$\lambda_c^{rel} = \frac{3}{2} \left(1 + \frac{P_*}{\epsilon_1} \right)$$



Heinmann, Hempel, Thielemann, Physical Review D, 94, 10, 2016



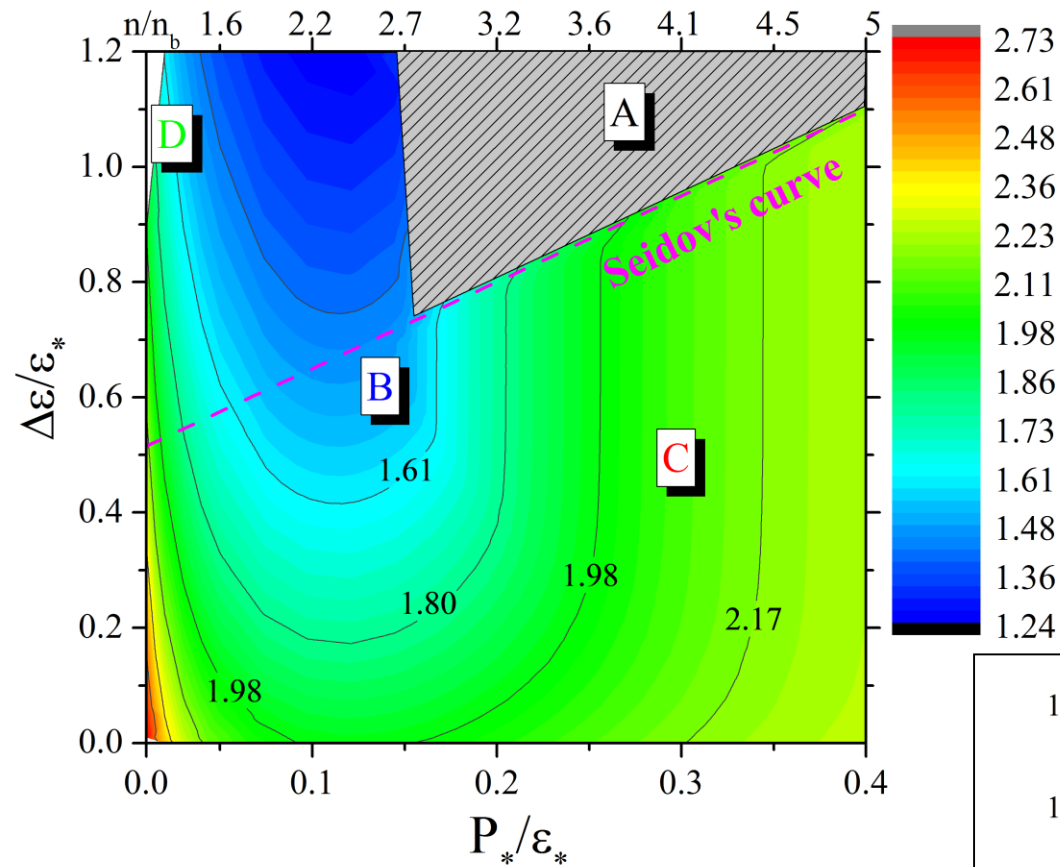
A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

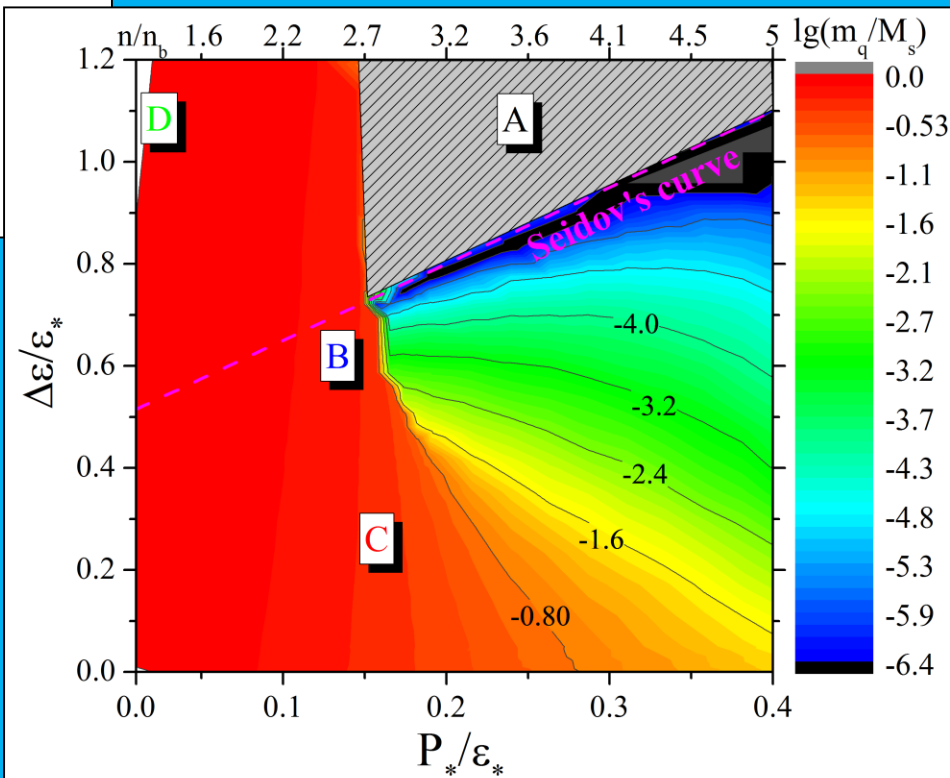
$$(1.97 \pm 0.04) M_{\odot}$$

Maximum mass M_s

← level lines



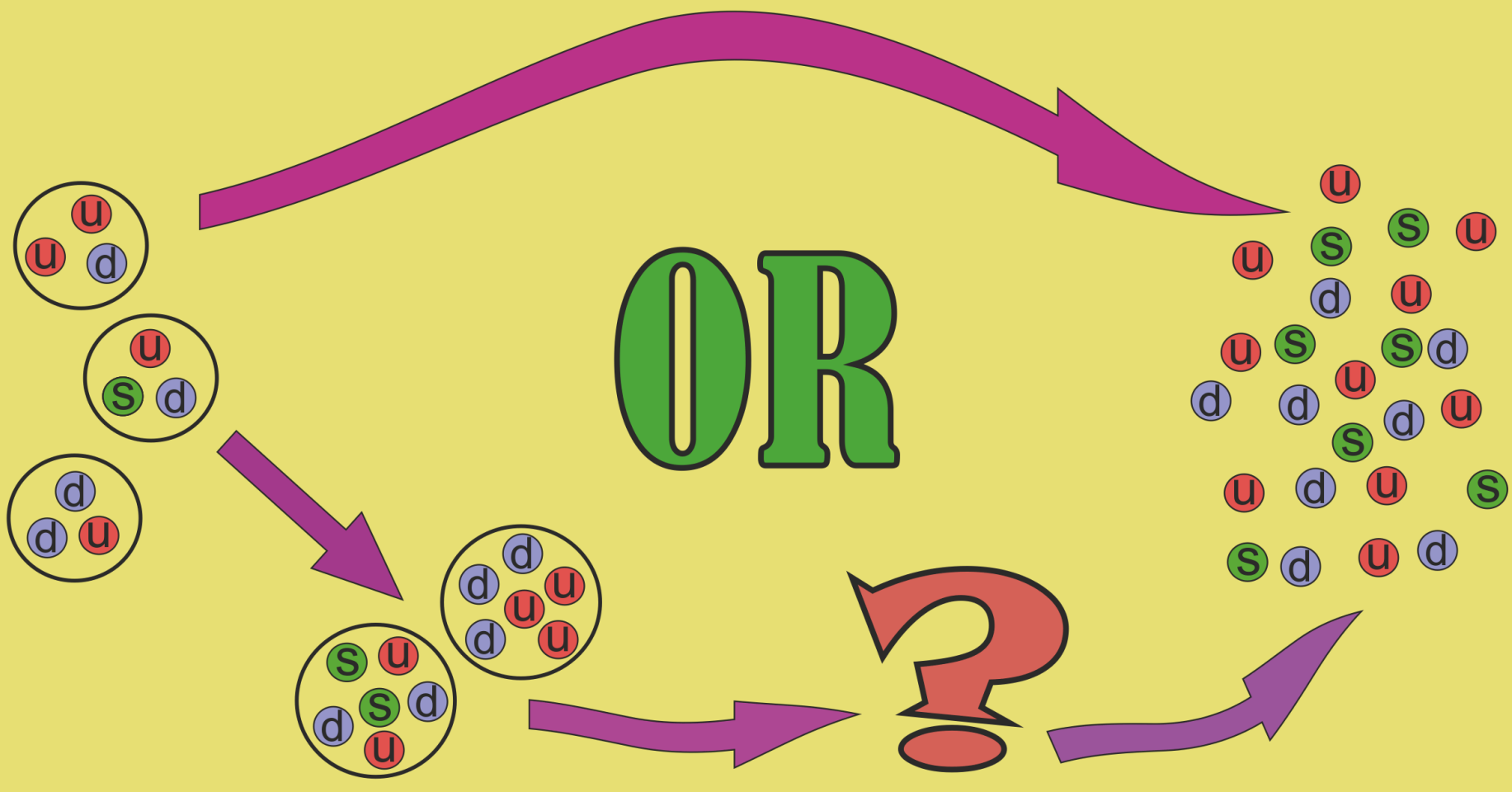
Log of mass fraction
of quark core $\log(m_q/M_s)$
level lines →



Phase transition from nuclear to quark matter: is it a single strong event or a series of weaker transitions?

NUCLEAR MATTER AT HIGH DENSITY: PHASE TRANSITIONS, MULTIQUARK STATES, AND SUPERNOVA OUTBURSTS

© 2011 M. I. Krivoruchenko, D. K. Nadyozhin, T. L. Rasinkova, Yu. A. Simonov, M. A. Trusov*, A. V. Yudin



Variational Principle

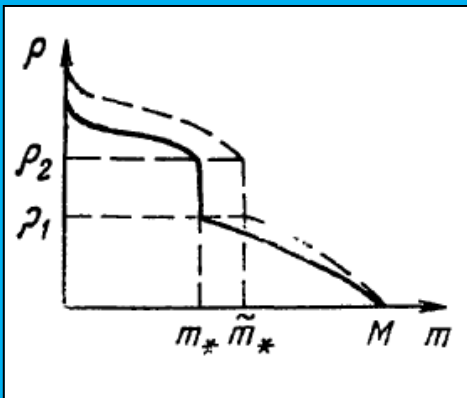
$$E_{tot} = E_{int} + W_G = \int \varepsilon_{int} dm - \int \frac{Gm}{r} dm = \min$$

Zel'dovich, Novikov
"Relativistic Astrophysics"

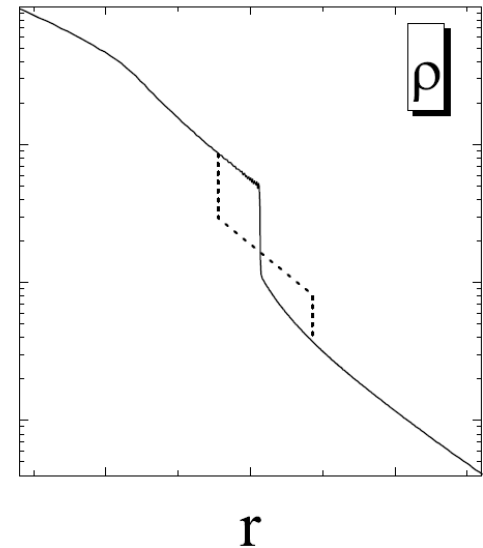
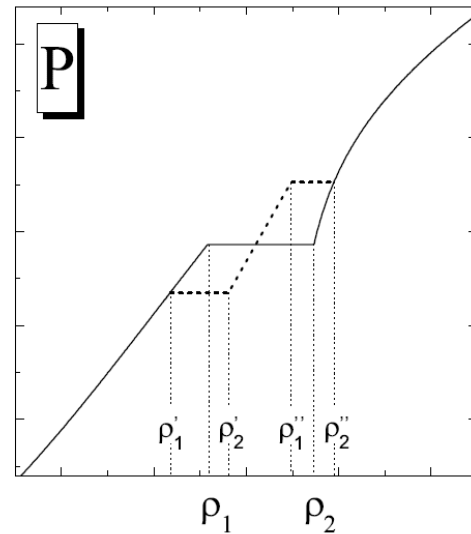
$$\delta E_{tot} = 0, \quad \delta^2 E_{tot} > 0$$

Bisnovatyi-Kogan,
Blinnikov, Shnol
Sov. Astron, 19, 559,1976

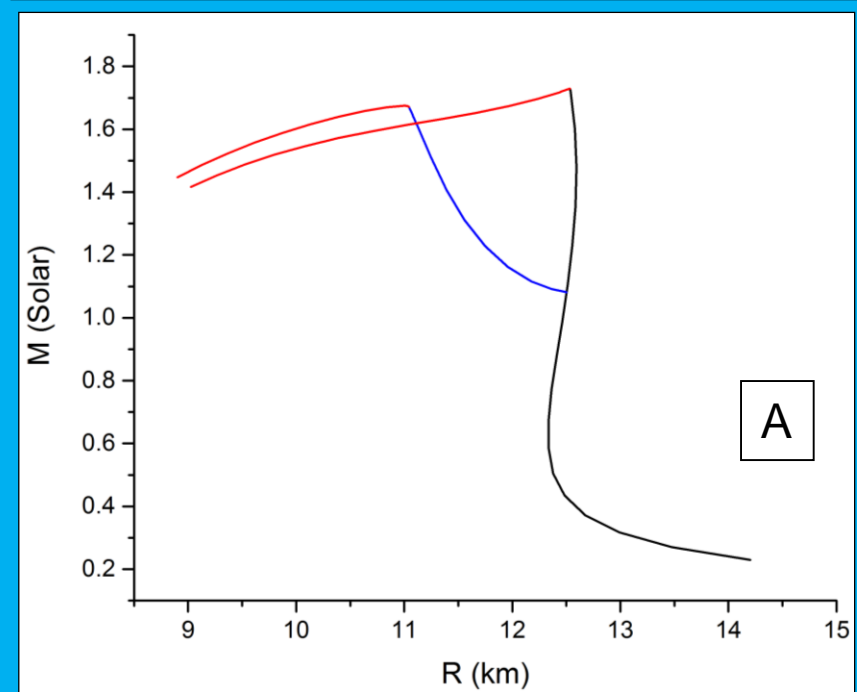
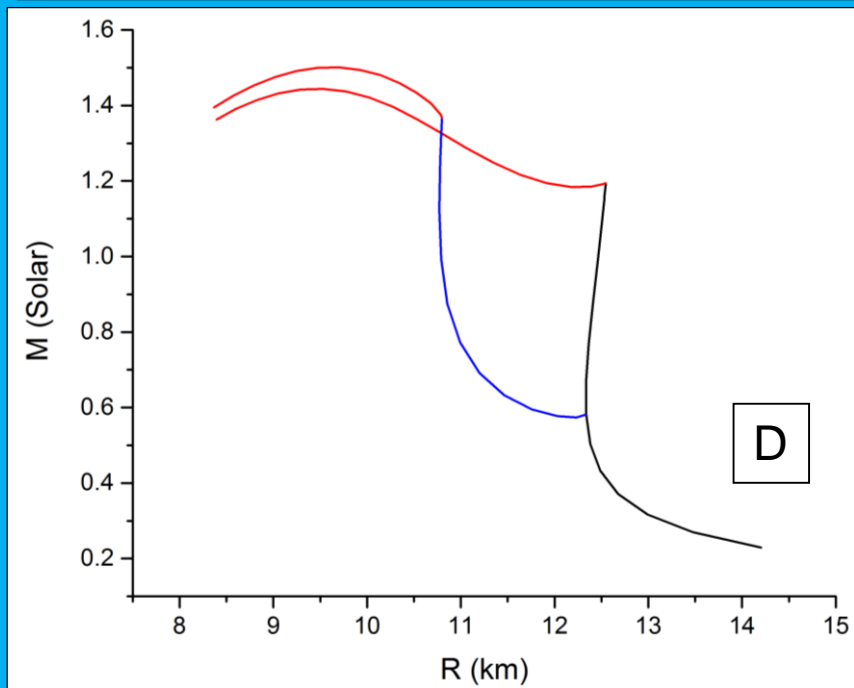
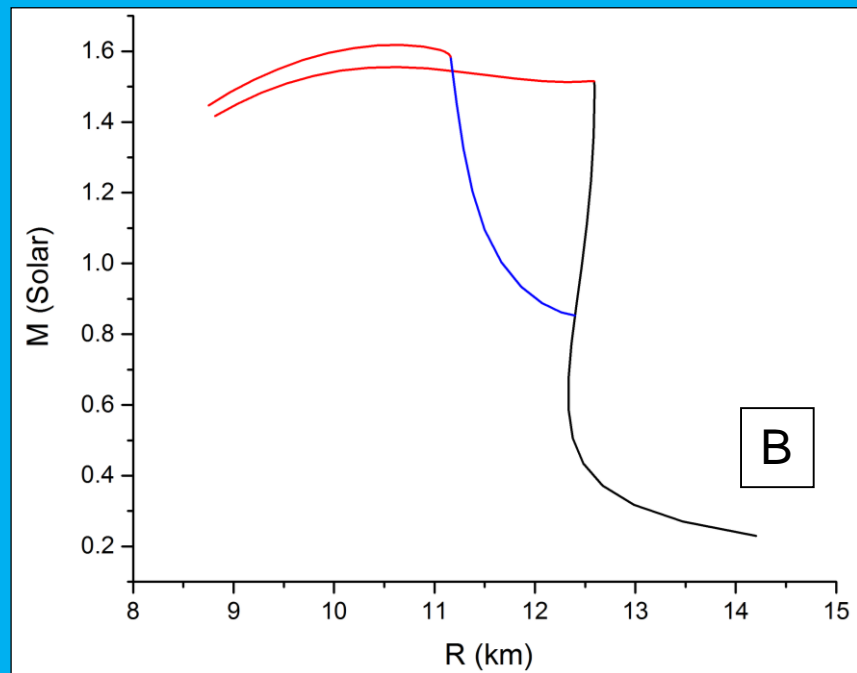
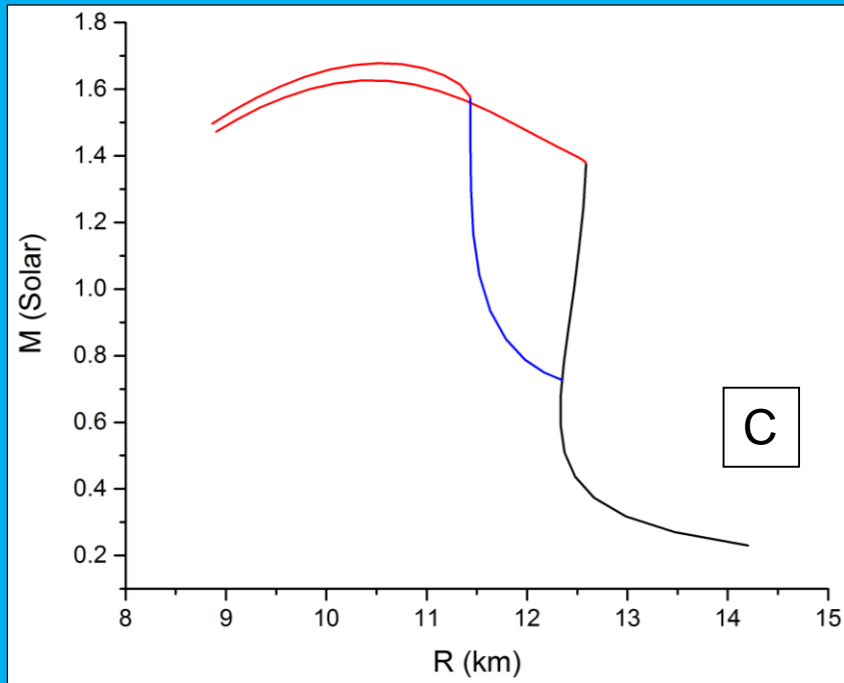
$$V = V_I + V_O = \int_0^M \left[P\gamma\rho \left(\frac{d\varphi}{dm} \right)^2 - \frac{4\beta m\varphi^2}{9 v^{7/3}} \right] dm + \frac{\beta m_*}{3v_*^{4/3}} \frac{(\varphi_1 - \varphi_2)^2}{\frac{1}{\rho_1} - \frac{1}{\rho_2}} > 0,$$

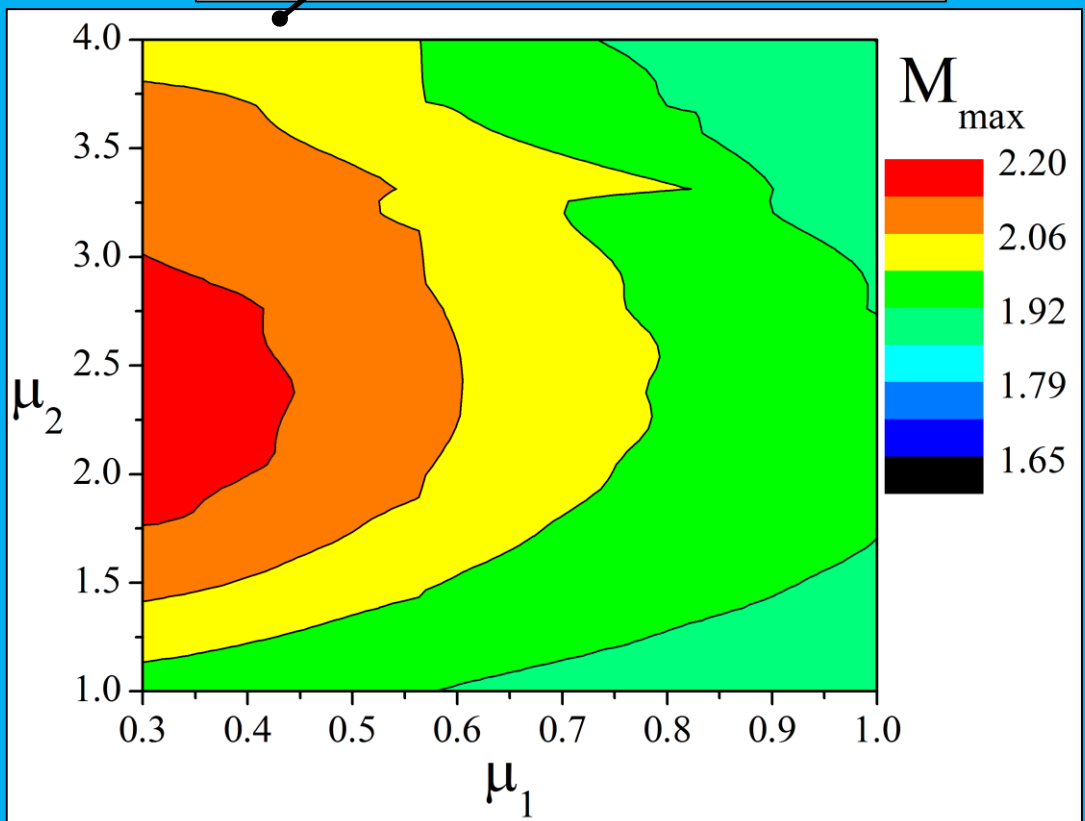
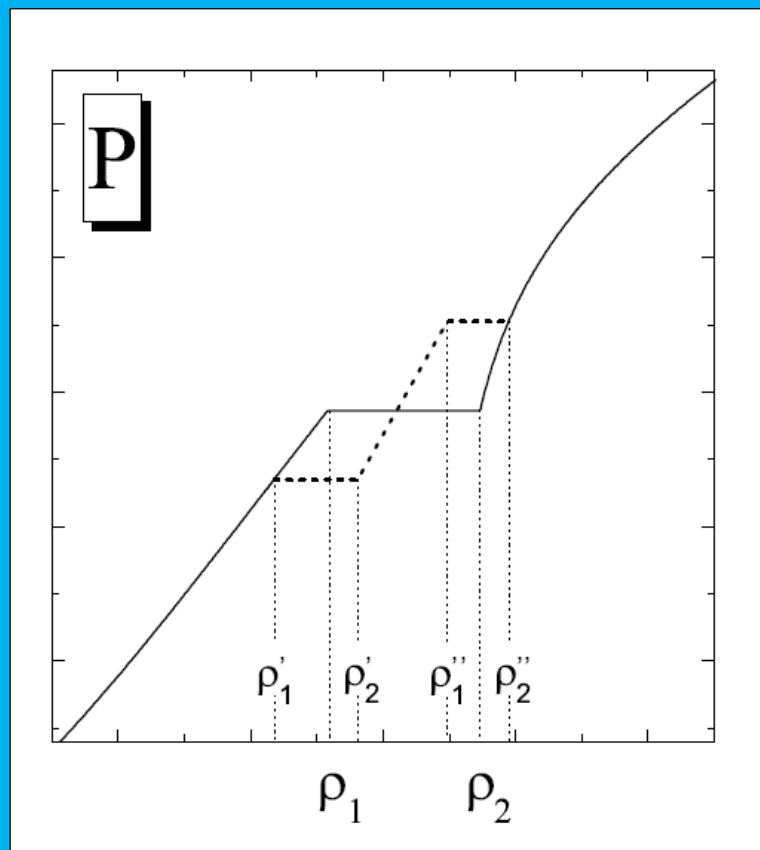
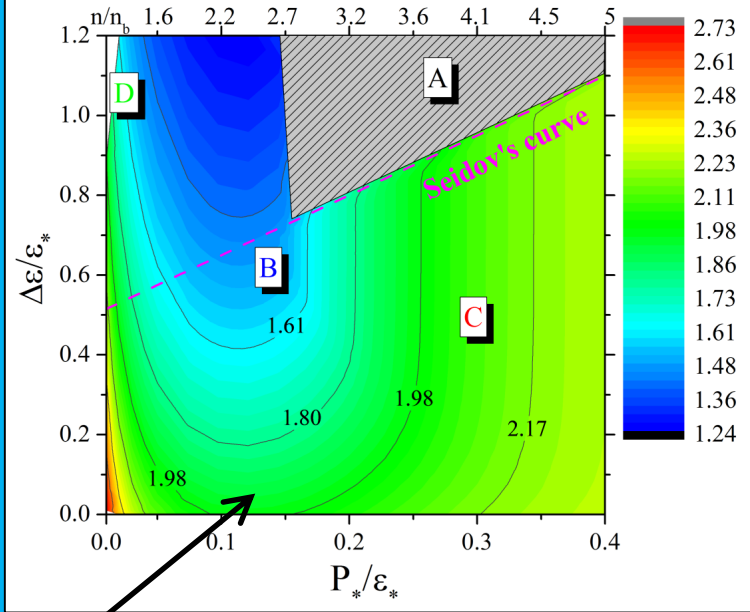


$$\frac{\rho_2}{\rho_1} < \frac{3}{2}$$



$$V'_O \propto \frac{(\varphi_1 - \varphi_3)^2}{\frac{1}{\rho_1} - \frac{1}{\rho_2'}} + \frac{(\varphi_3 - \varphi_2)^2}{\frac{1}{\rho_1''} - \frac{1}{\rho_2}} \geq \frac{(\varphi_1 - \varphi_2)^2}{\frac{1}{\rho_1} - \frac{1}{\rho_2}}$$

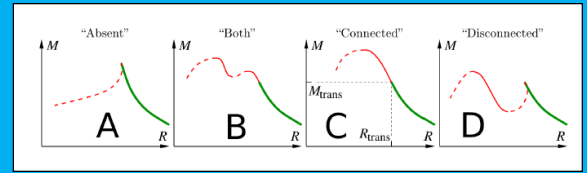




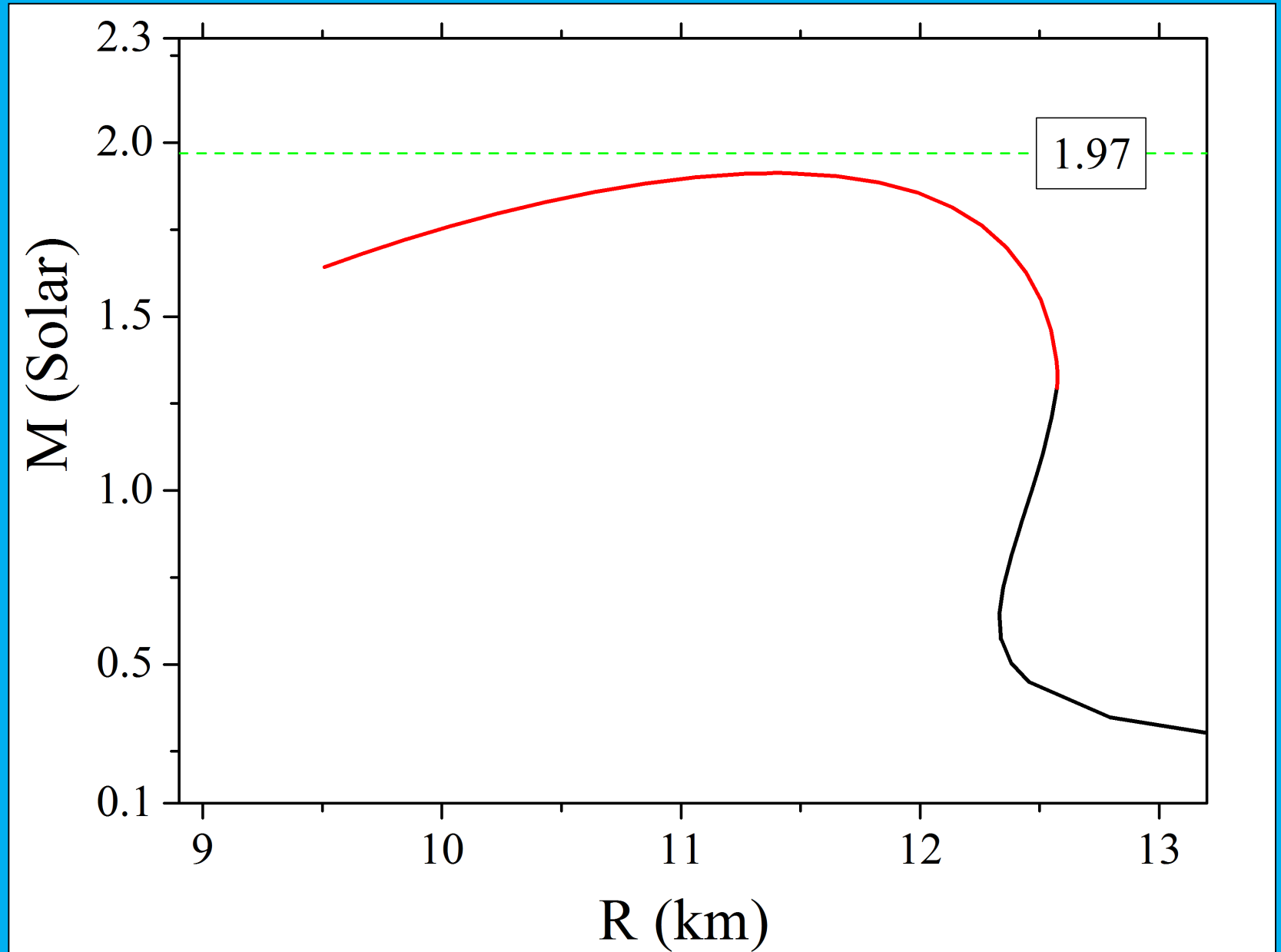
$$\rho_1' = \rho_1 \times \mu_1, \quad \mu_1 \leq 1$$

$$\rho_2'' = \rho_2 \times \mu_2, \quad \mu_2 \geq 1$$

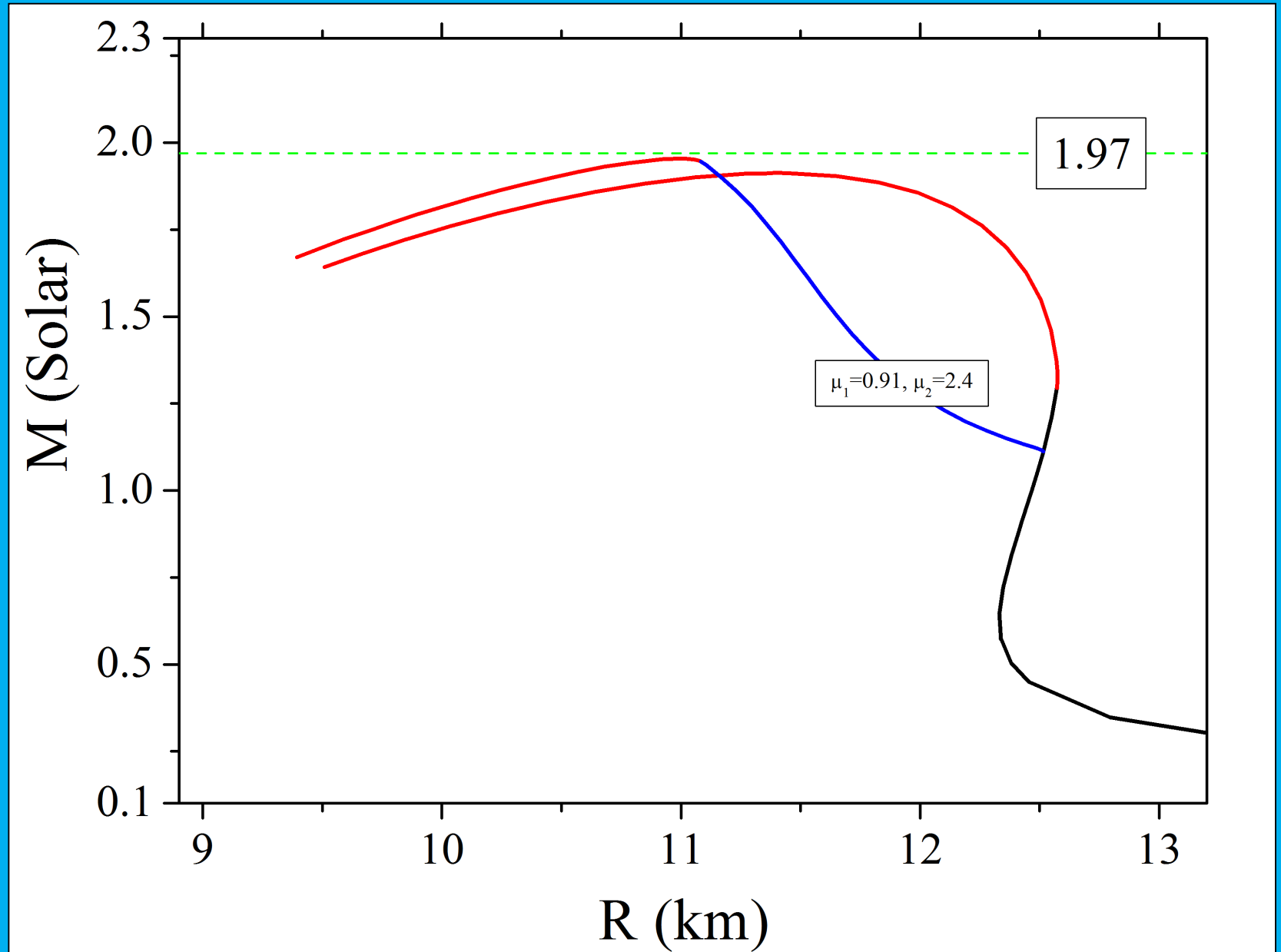
$M_{\max}(1PT) = 1.91 M_{\text{Sun}}$



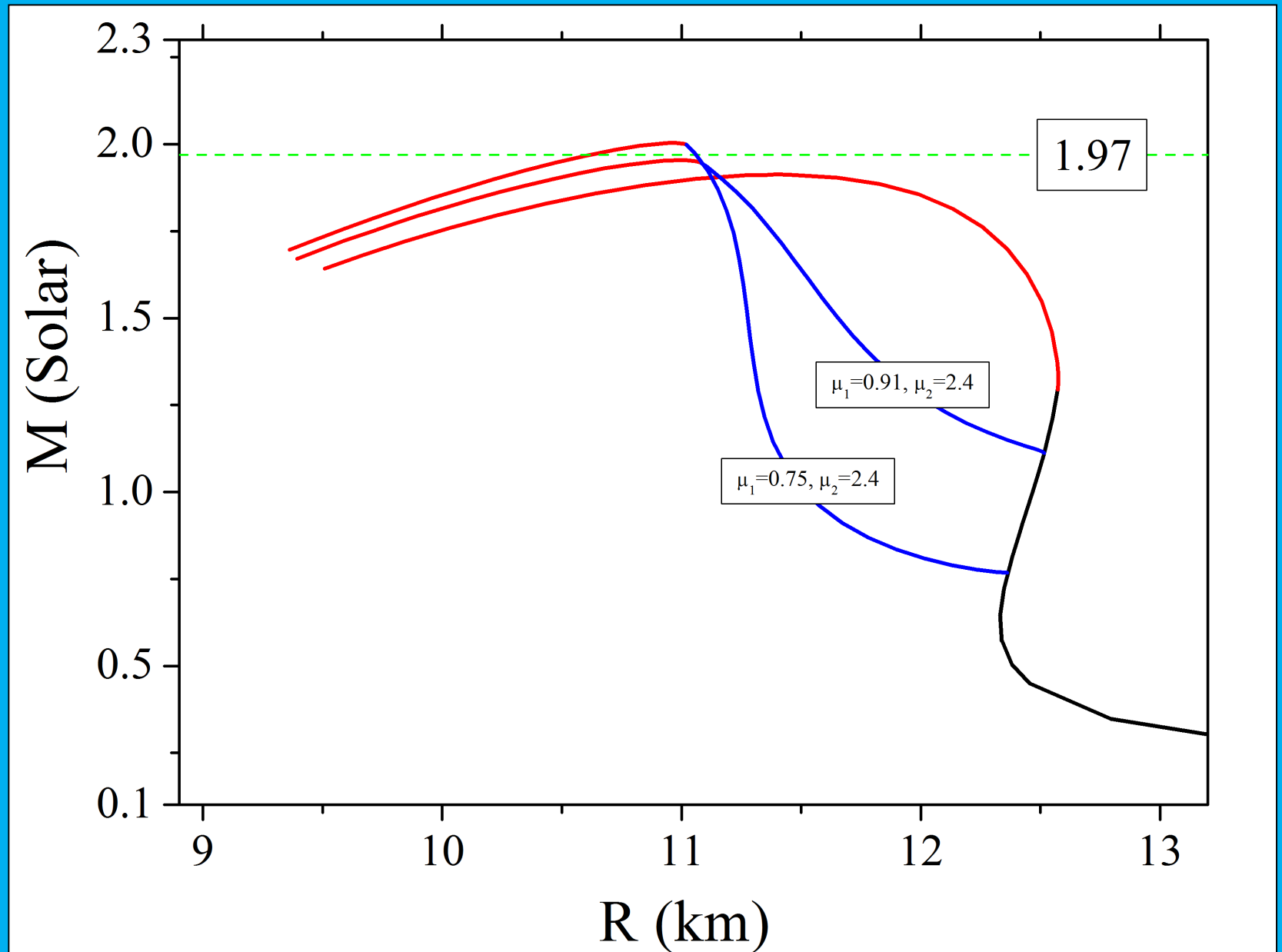
Mass-Radius relation



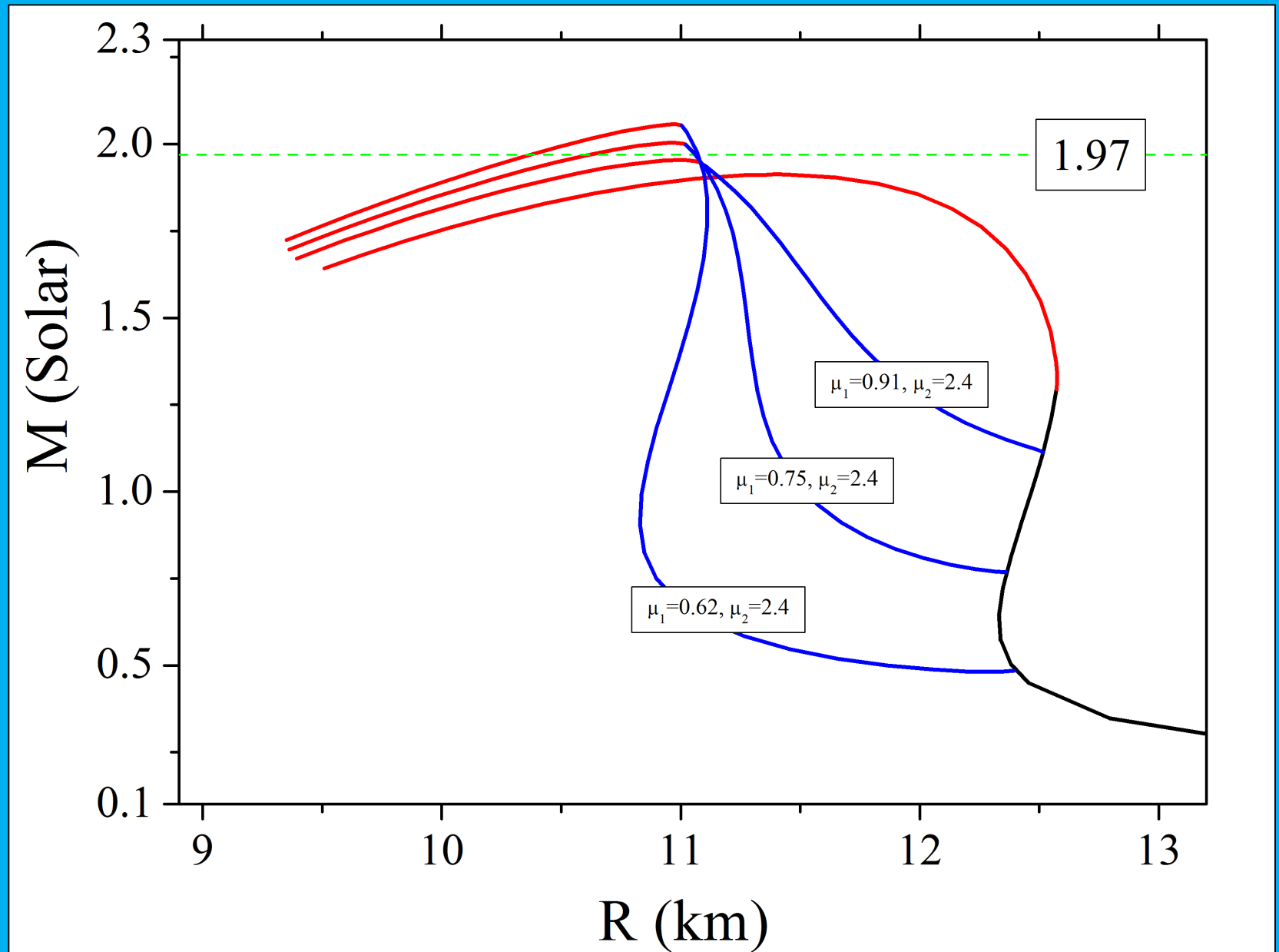
Mass-Radius relation



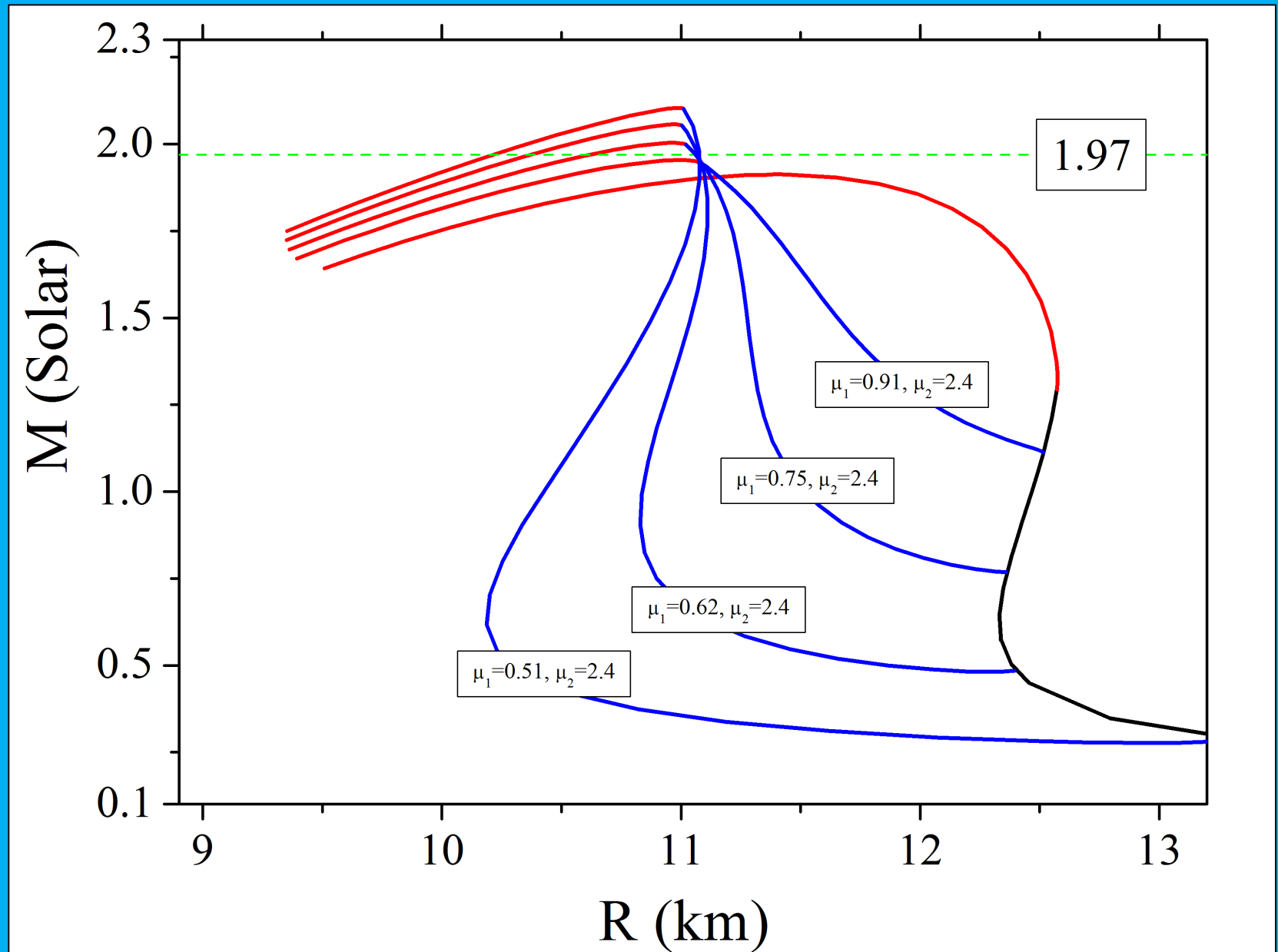
Mass-Radius relation



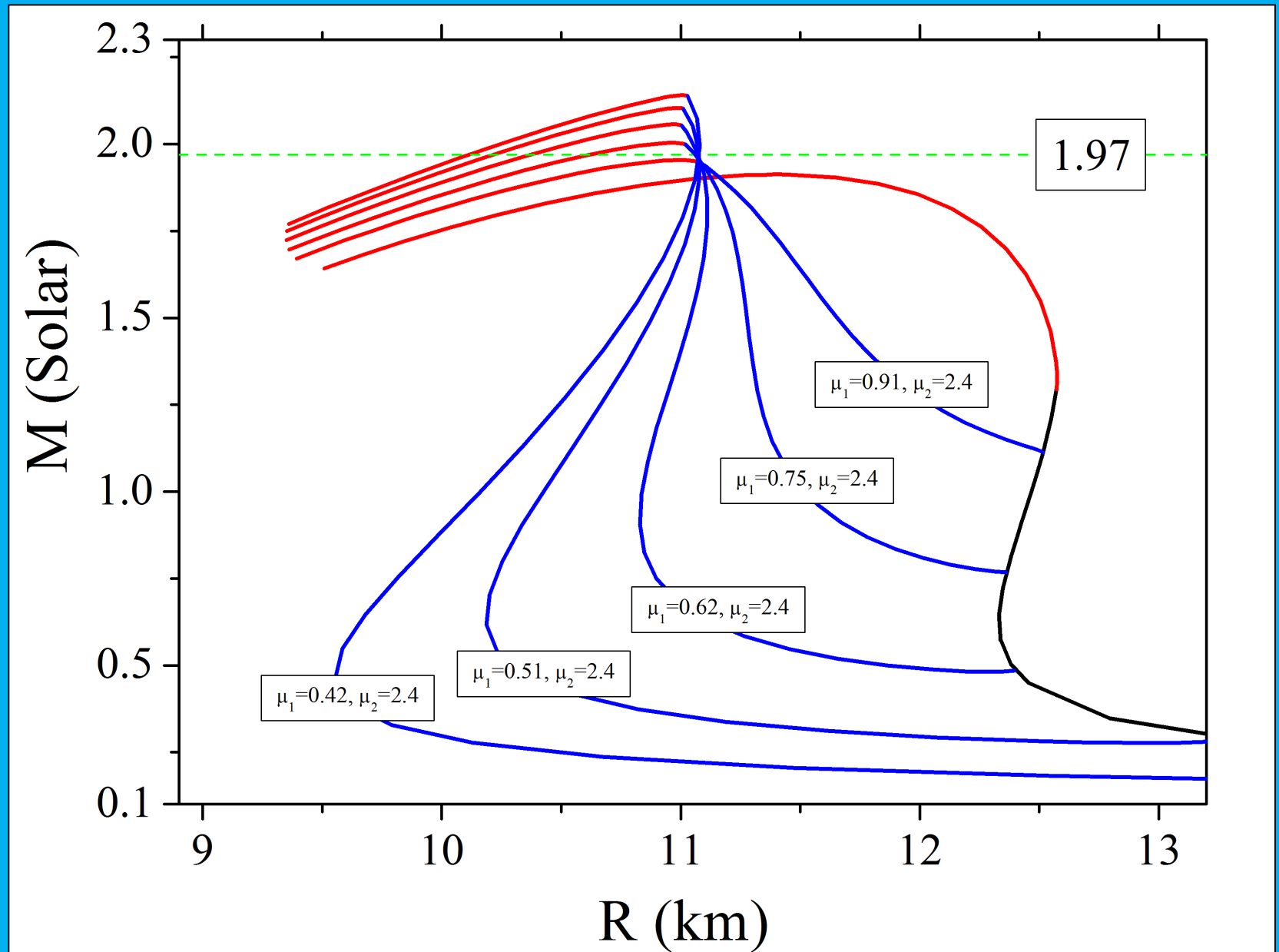
Mass-Radius relation



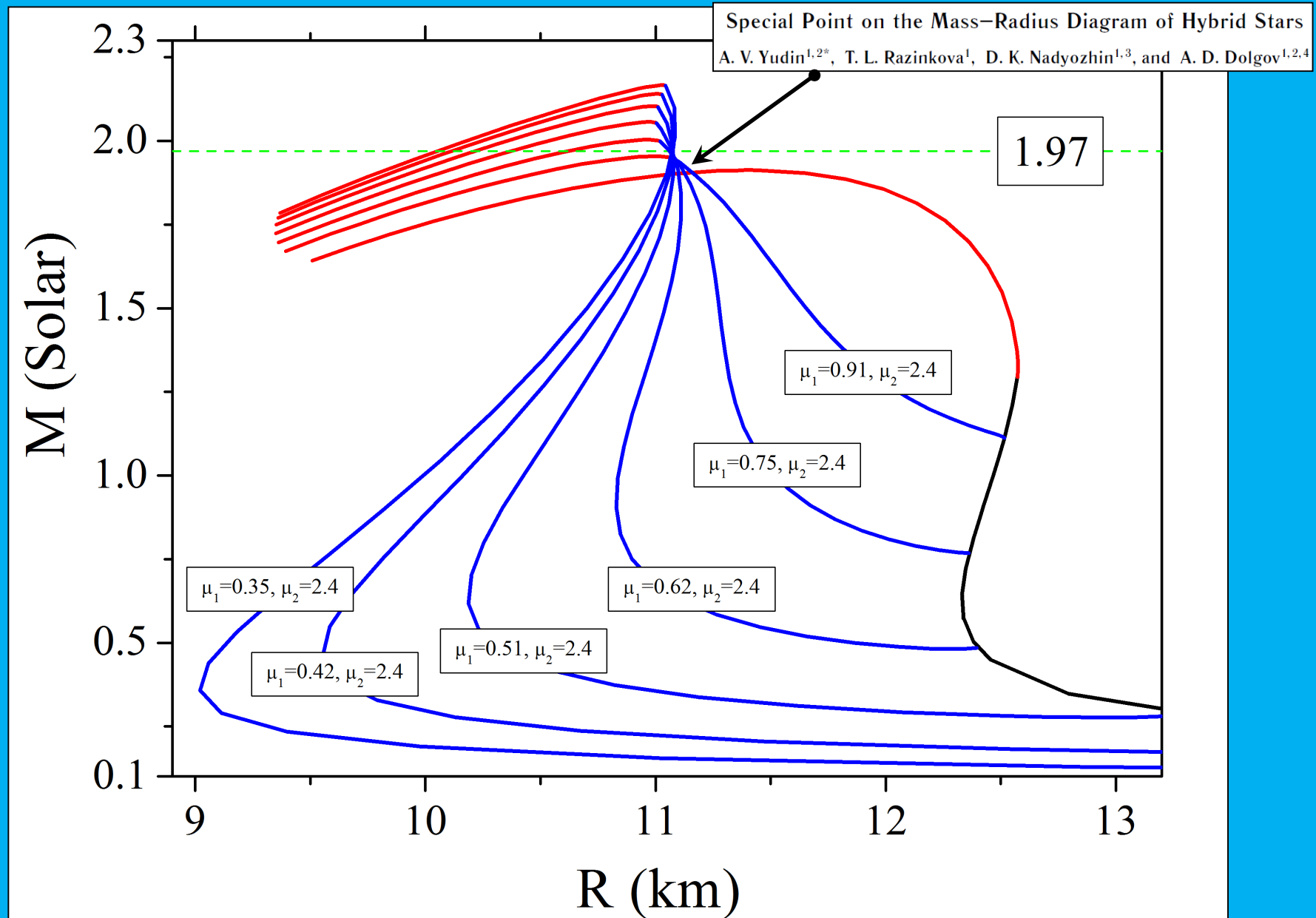
Mass-Radius relation

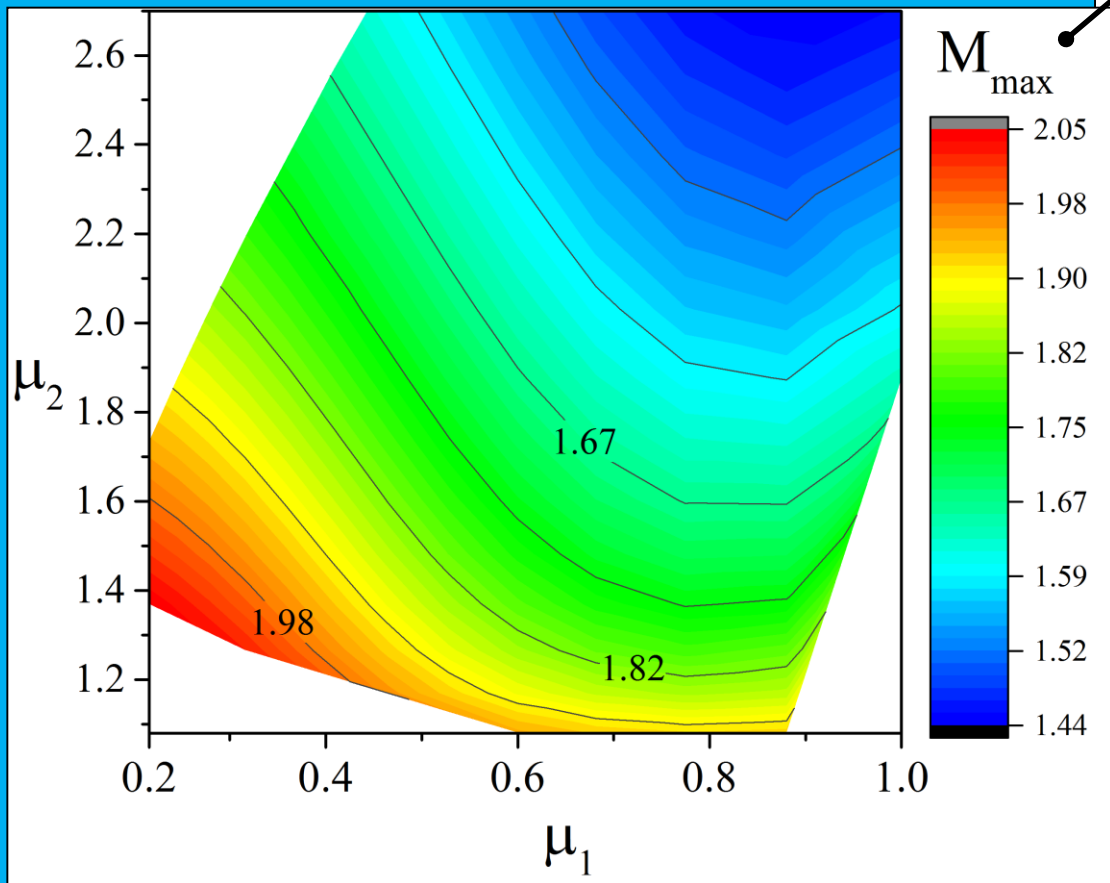
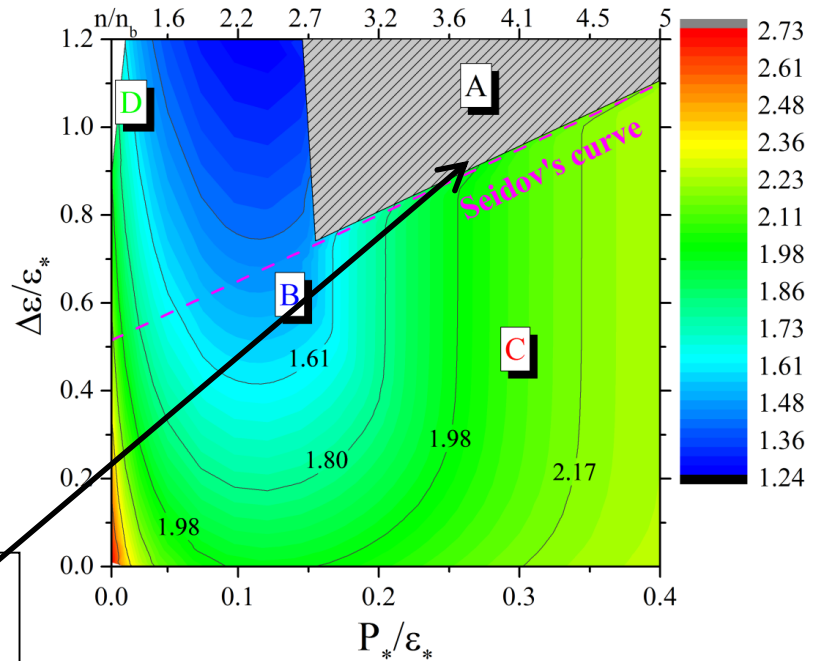
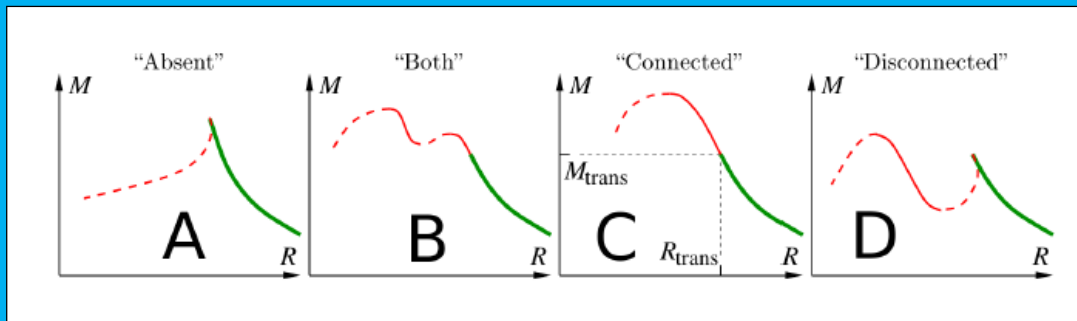


Mass-Radius relation

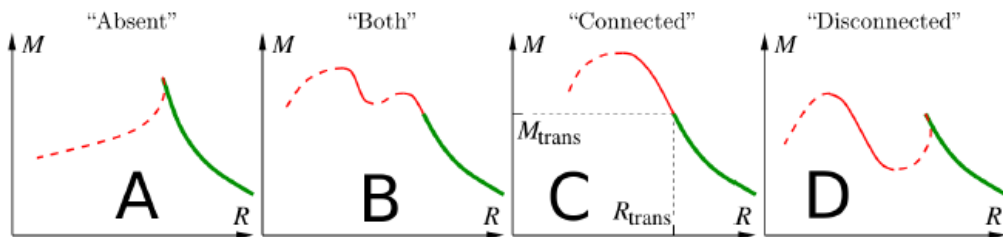


Mass-Radius relation

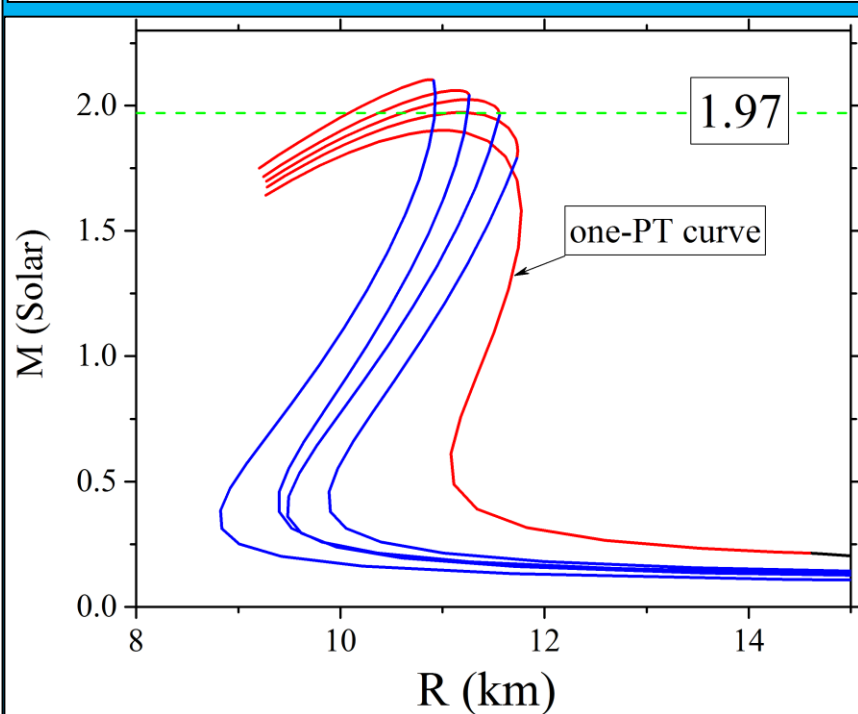
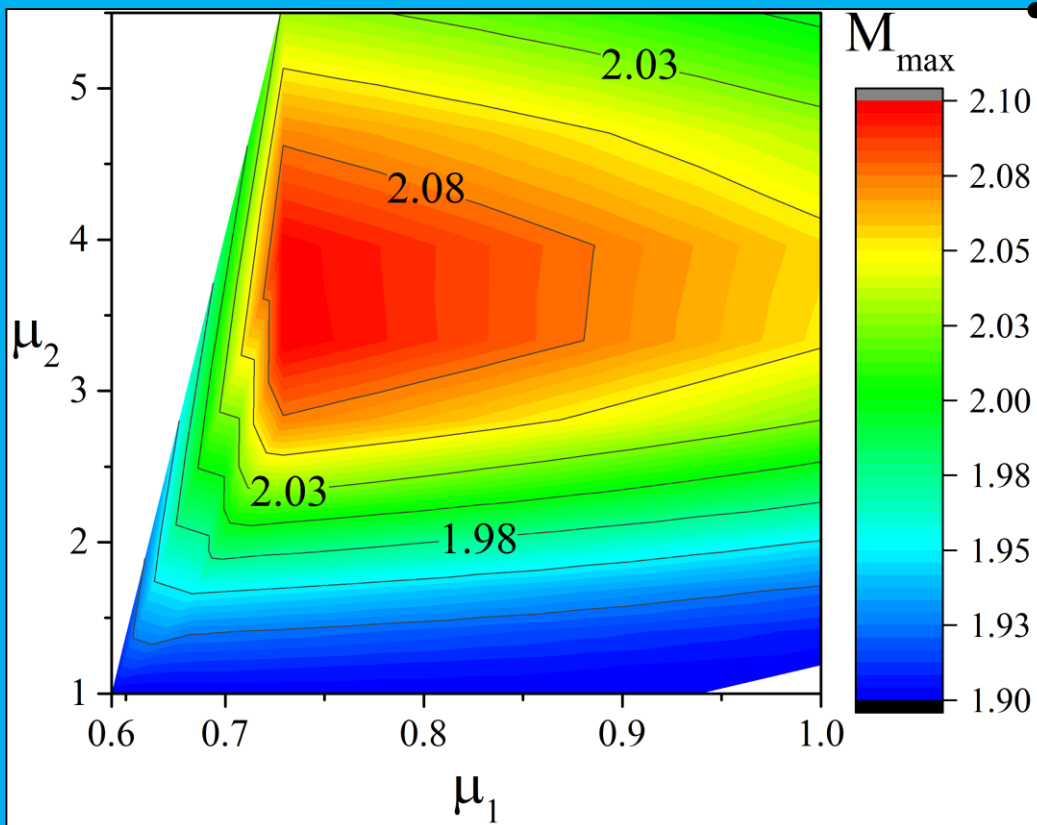
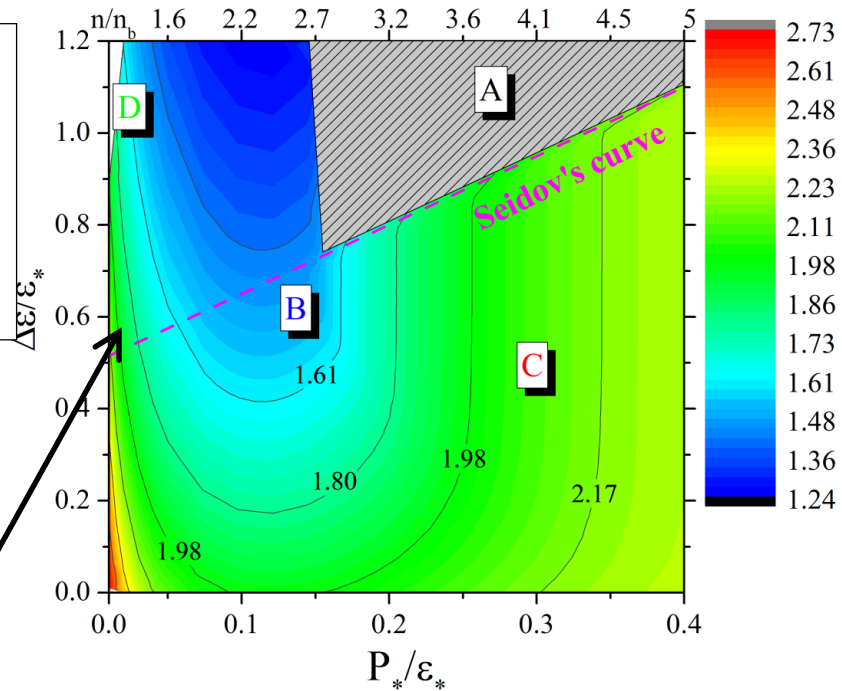




**$M_{\text{max}}(1\text{PT}) = 2.0 M_{\text{sun}}$
but no stable hybrid configurations!**



$M_{\text{max}}(1\text{PT}) = 1.9 M_{\text{sun}}$



Quark/hybrid stars

The scenario of two families of compact stars

1. Equations of state, mass-radius relations and binary systems

Alessandro Drago¹, Andrea Lavagno², Giuseppe Pagliara¹, and Daniele Pigato²

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2. Transition from hadronic to quark matter and explosive phenomena

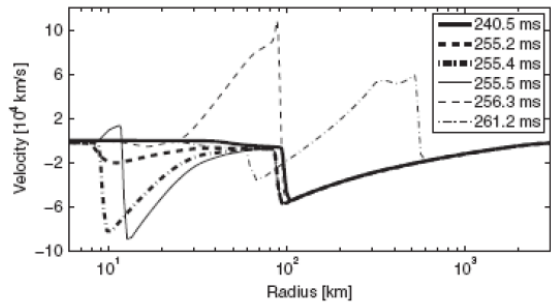
Alessandro Drago and Giuseppe Pagliara

PRL 102, 081101 (2009) PHYSICAL REVIEW LETTERS week ending 27 FEBRUARY 2009

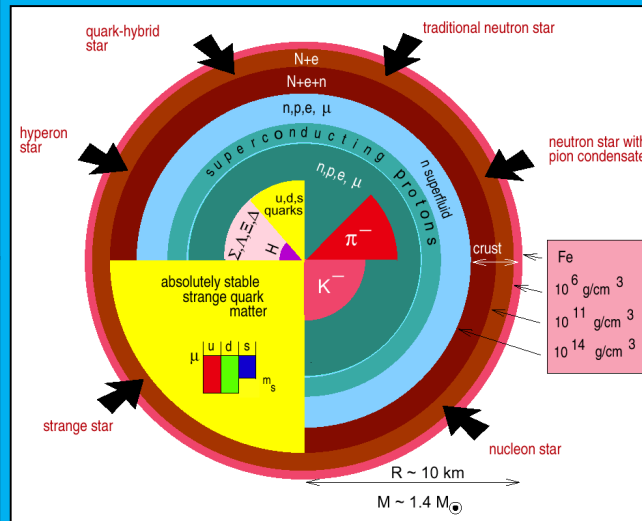
Signals of the QCD Phase Transition in Core-Collapse Supernovae

I. Sagert,¹ T. Fischer,³ M. Hempel,¹ G. Pagliara,² J. Schaffner-Bielich,³ A. Mezzacappa,⁴ F.-K. Thielemann,⁵ and M. Liebendörfer²

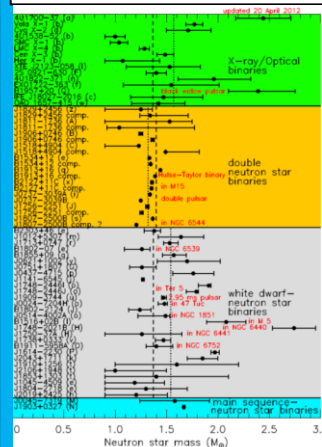
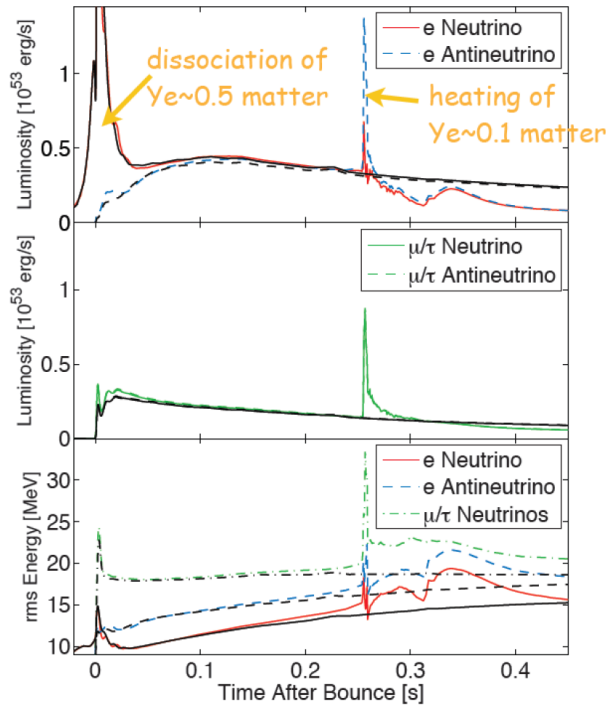
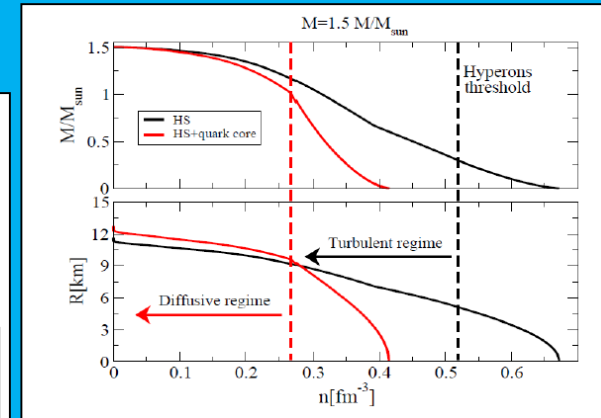
SN-hybrid star connection



Properties of compact stars



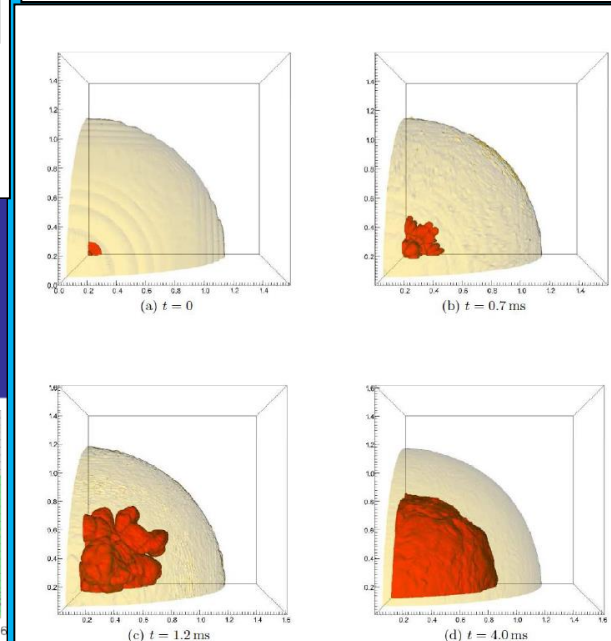
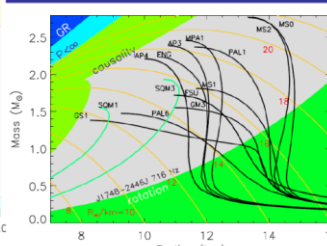
Quark star formation



Maximum neutron star mass

J.M. Lattimer

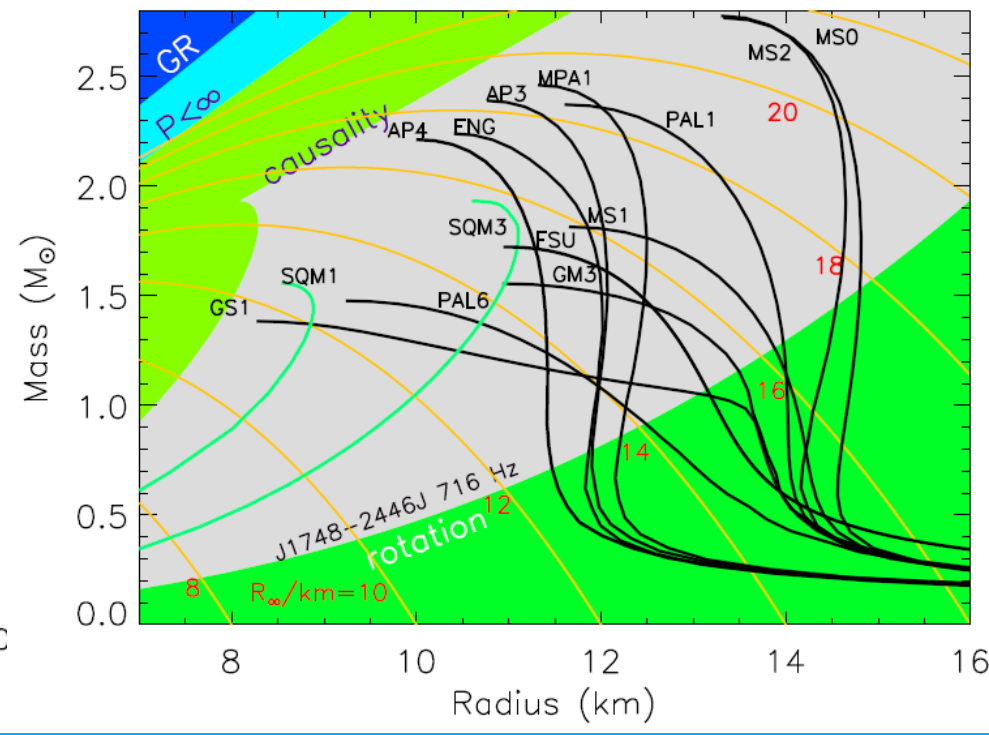
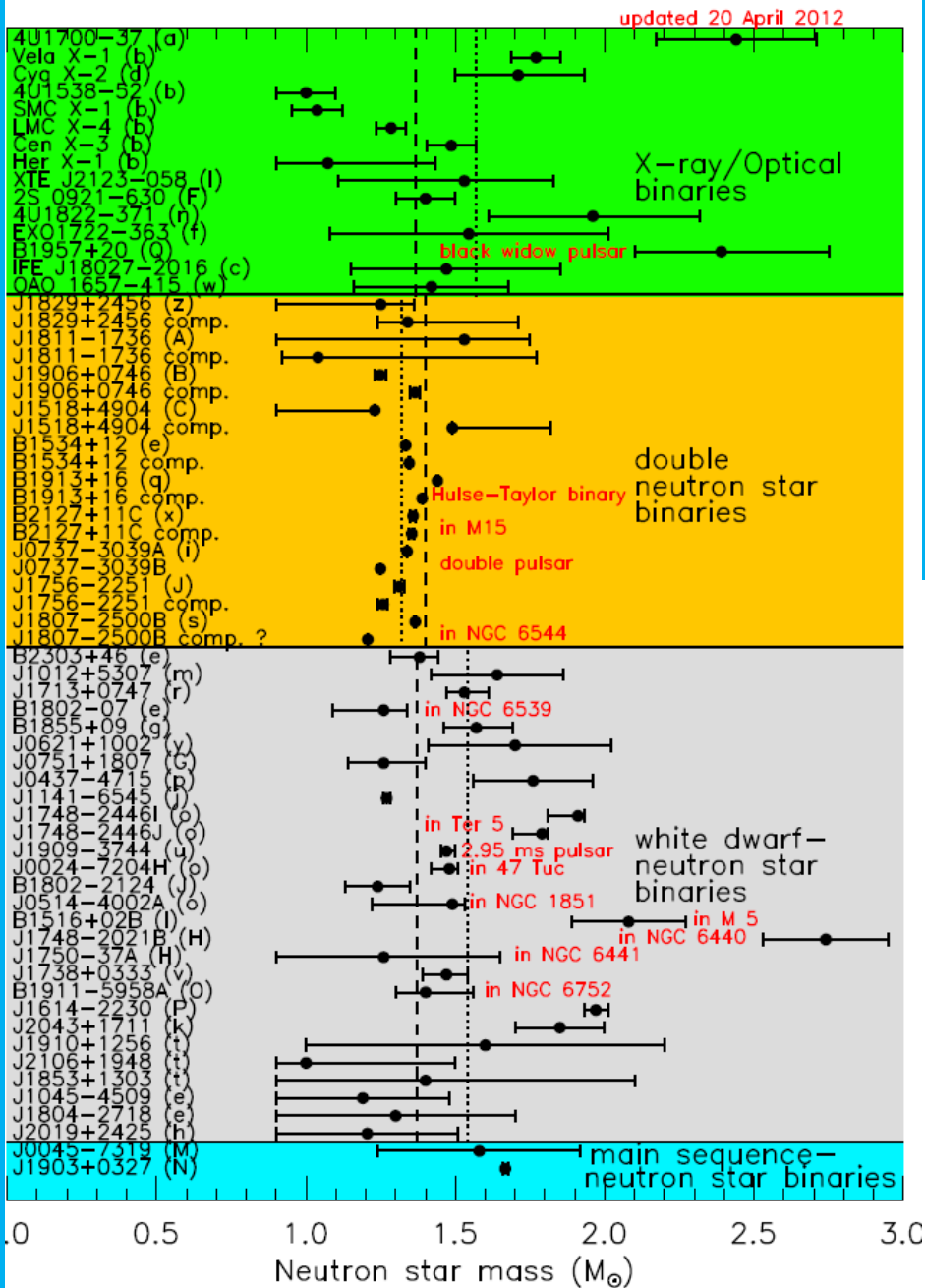
Annual Review of Nuclear and Particle Science, vol. 62, issue 1, pp. 485-515 (2012)



Maximum neutron star mass

J.M. Lattimer

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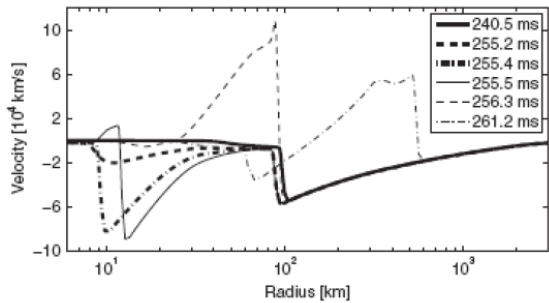
Alessandro Drago and Giuseppe Pagliara

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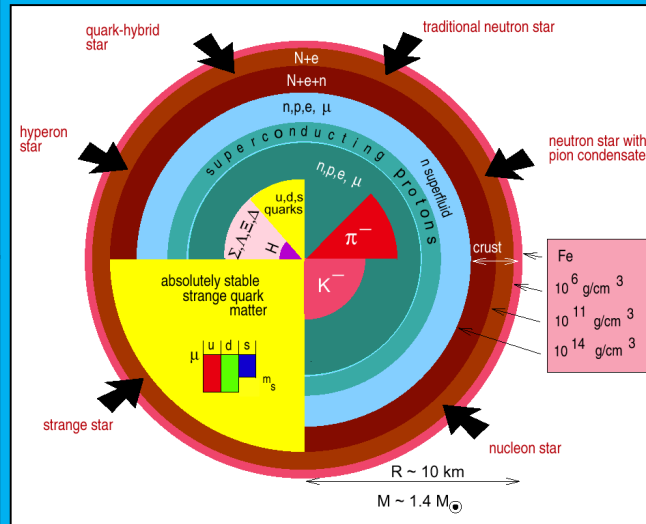
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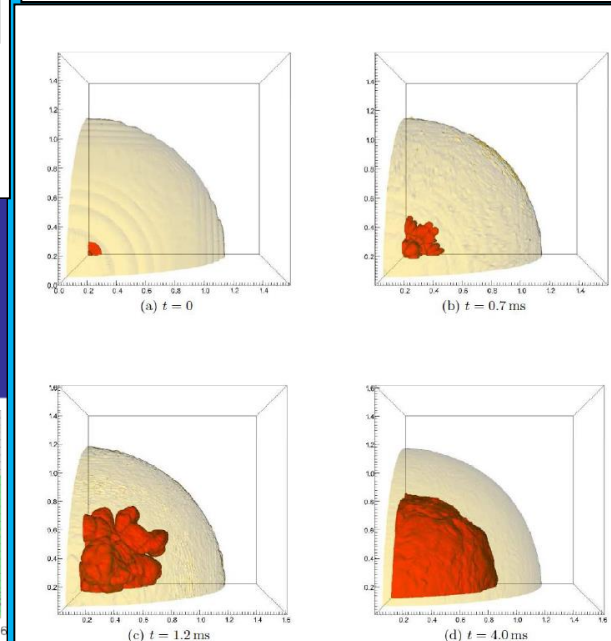
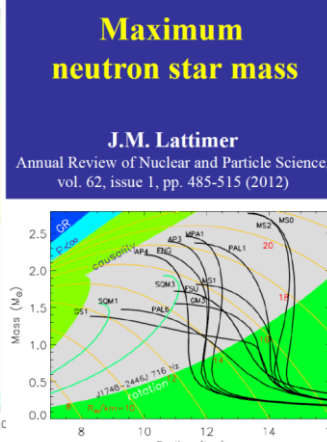
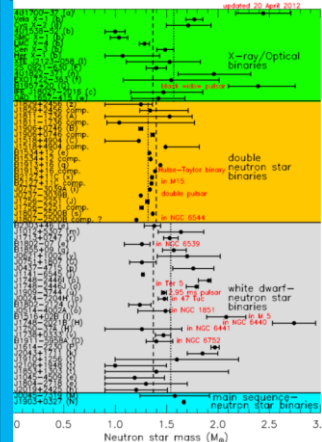
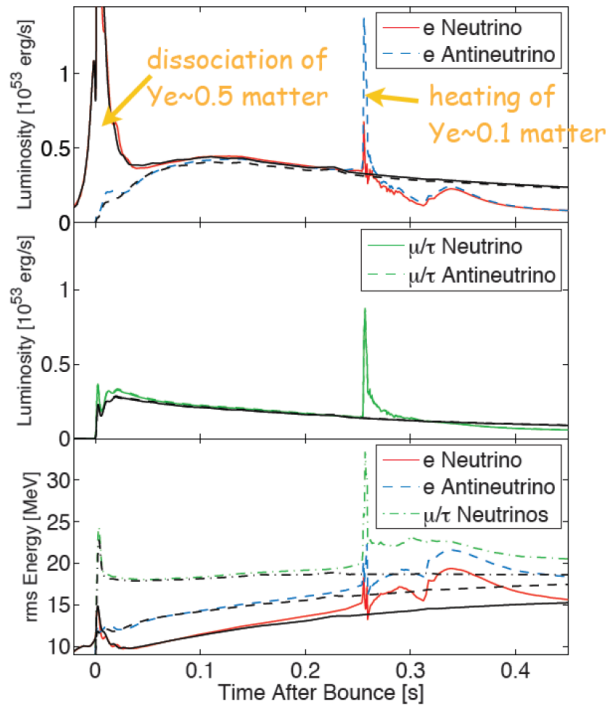
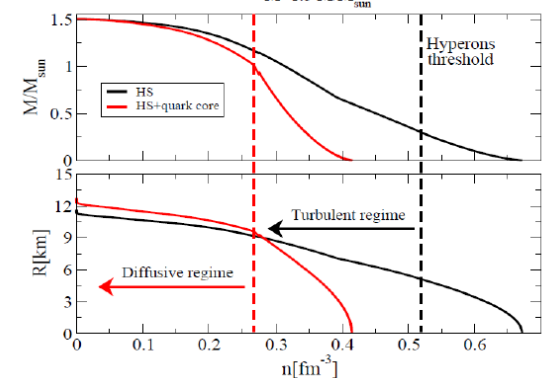
SN-hybrid star connection



Properties of compact stars



Quark star formation



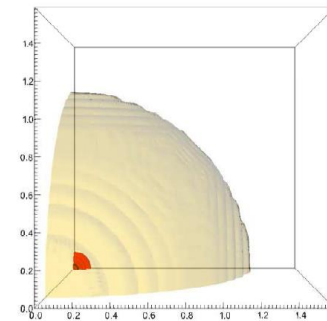
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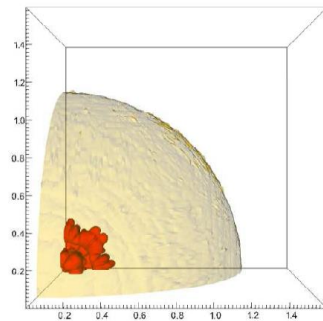
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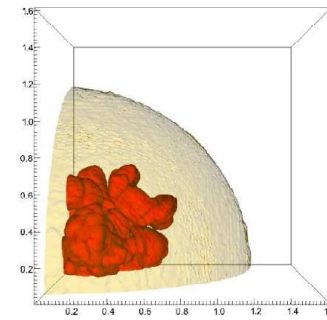
Alessandro Drago and Giuseppe Pagliara



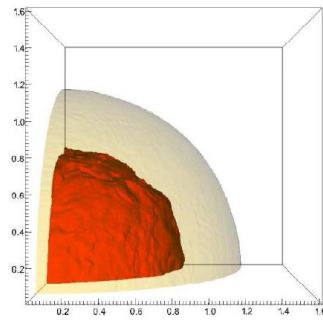
(a) $t = 0$



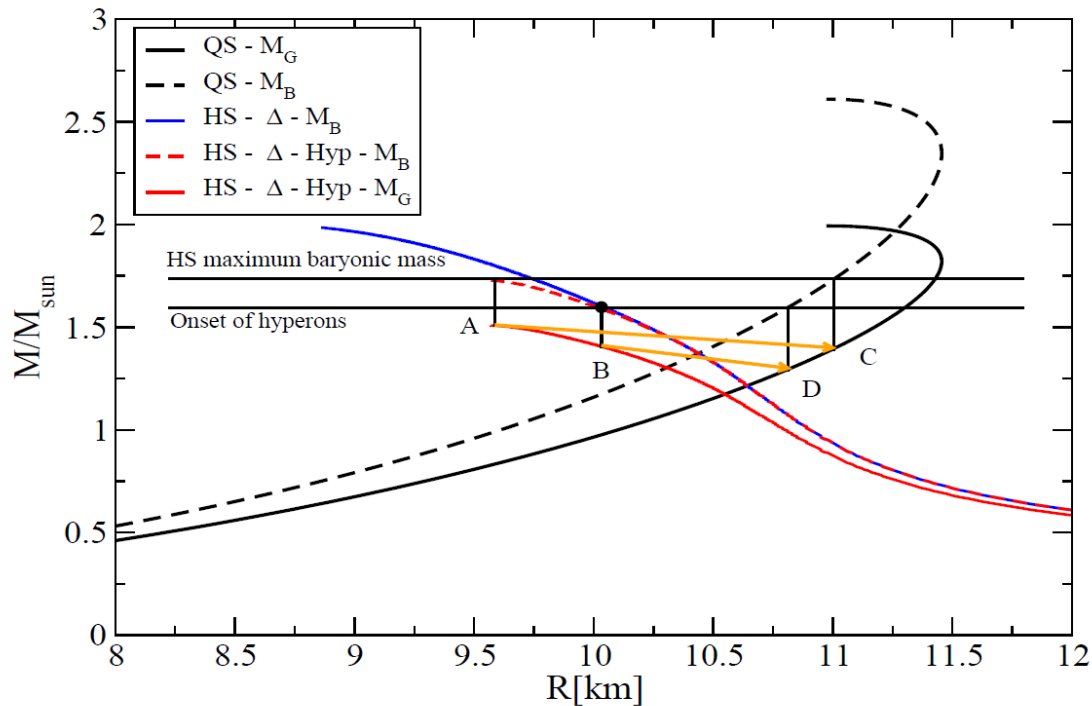
(b) $t = 0.7$ ms



(c) $t = 1.2$ ms



(d) $t = 4.0$ ms



Quark/hybrid stars

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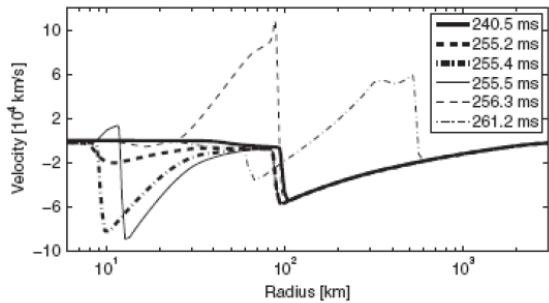
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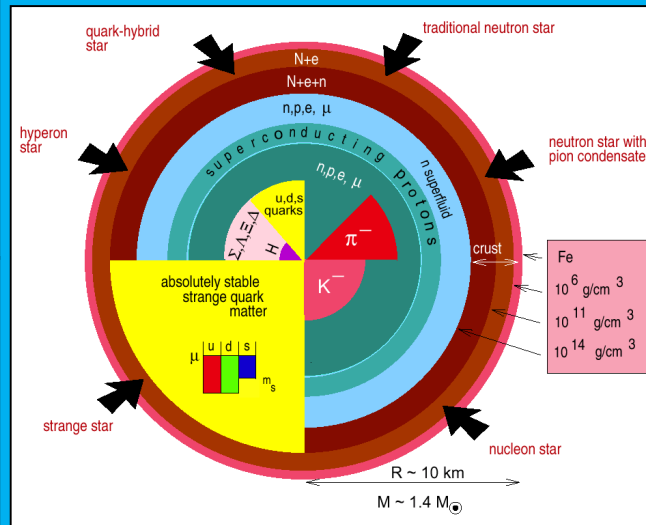
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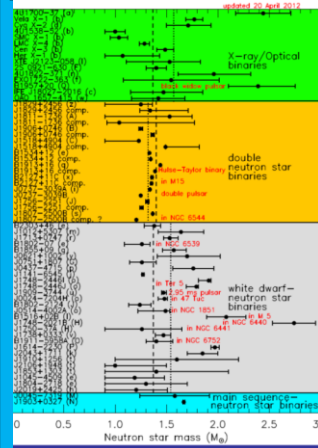
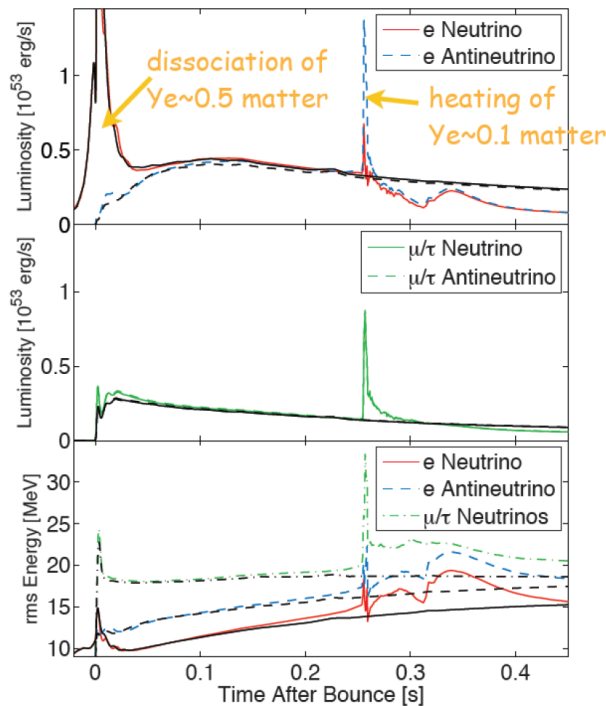
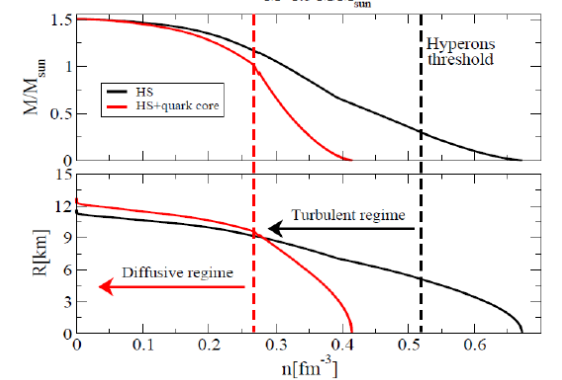
SN-hybrid star connection



Properties of compact stars



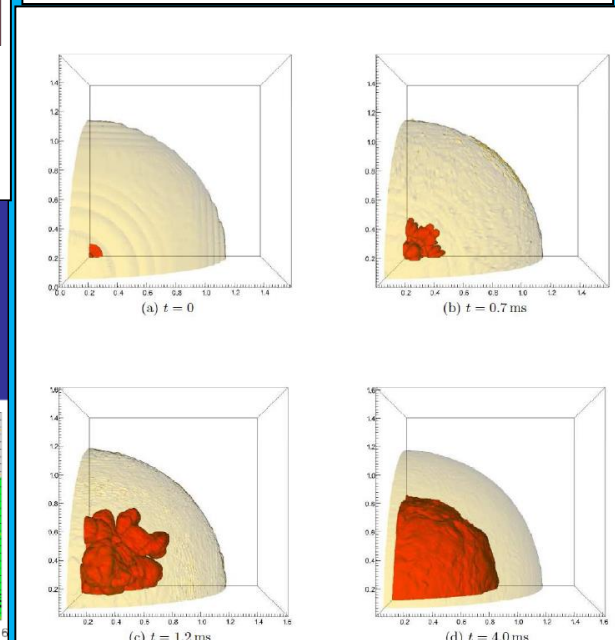
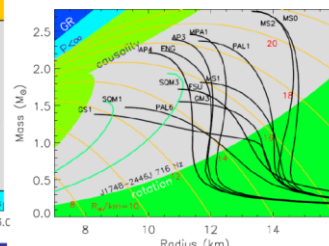
Quark star formation



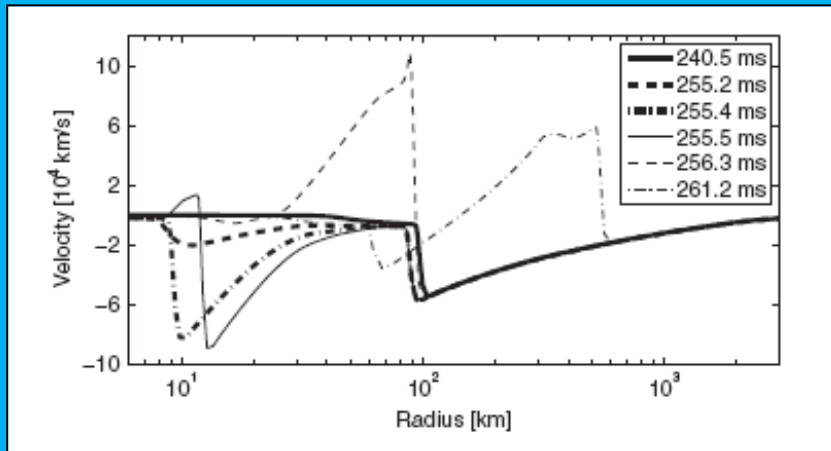
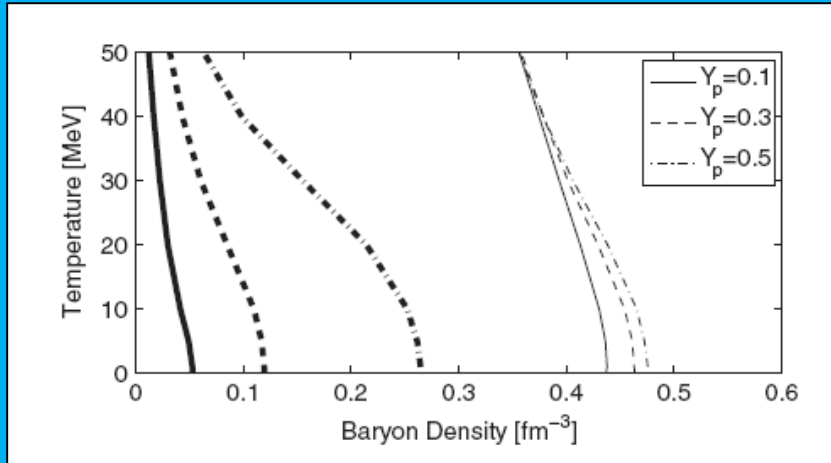
Maximum neutron star mass

J.M. Lattimer

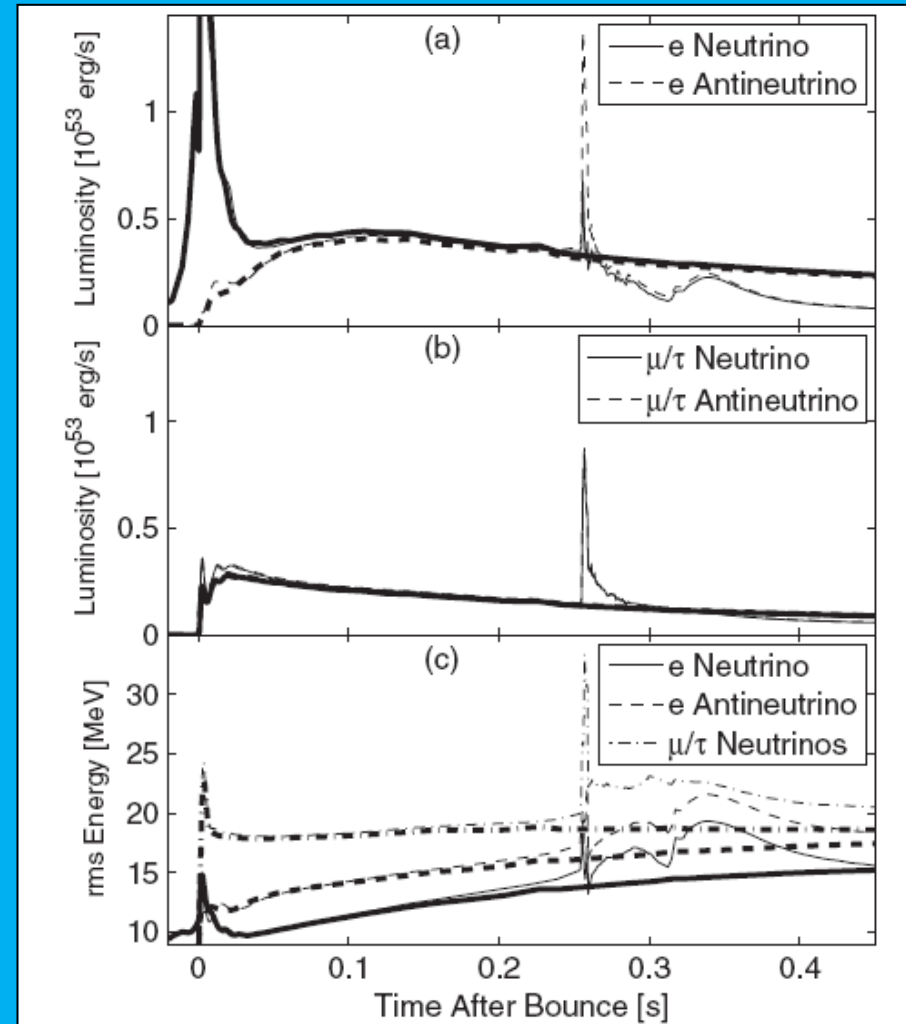
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Signals of the QCD Phase Transition in Core-Collapse Supernovae

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Prog.	EOS	t_{pb}	M_Q	M_{mix}	M_{pns}	E_{expl}	BE	M_G
[M_\odot]		[ms]	[M_\odot]	[M_\odot]	[M_\odot]	[10^{51} erg]	[10^{53} erg]	[M_\odot]
10	<i>eos1</i>	255	0.850	0.508	1.440	0.44	3.40	1.25
10	<i>eos2</i>	448	1.198	0.161	1.478	1.64	3.19	1.30
15	<i>eos1</i>	209	1.146	0.320	1.608	0.42	4.08	1.38
15	<i>eos2</i>	330 ^a	1.496	0.116	1.700	... ^b	4.28	1.46

^amoment of black hole formation^bblack hole formation before explosion



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Thank you !

